

1 **Football Quotient: Quantifying National**  
2 **Playing Ability**  
3 **and the Disproportionate Returns to**  
4 **Development Quality**  
5 **in European Professional Football**

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## Abstract

**Background.** A persistent empirical puzzle in European football is why small nations—notably Serbia, Croatia, and Scotland—produce professional players at rates far exceeding large, well-resourced nations such as Germany, France, and the Netherlands. Existing accounts cite culture and infrastructure, but lack a quantitative theoretical framework capable of making testable predictions.

**Methods.** We introduce the Football Quotient ( $FQ$ ), a latent-ability construct modelled as a normally distributed trait ( $\sigma = 15$ , analogous to the psychometric IQ scale), and derive the implied national mean  $FQ$  for 29 European nations from their senior professional player conversion rates. Player counts were obtained from Transfermarkt squad data for 2024/25, restricted to senior professionals (born  $\leq 2003$ ), and cross-validated against CIES Football Observatory reports. Registered player totals were compiled from FIFA Big Count supplemented by federation-level sources. Monte Carlo confidence intervals ( $n = 10,000$ ) propagated registration uncertainty.

**Results.** The pan-European conversion rate of 1.17 per 1,000 active players implies a professional threshold of  $FQ = 145.6$ . Implied national means range from Serbia (109.0; 95% CI 105.9–112.6) to Germany (96.5; 95% CI 95.5–97.4). Regression modelling of FIFA rankings ( $n = 29$ ) identified the number of professionals based abroad as the strongest single predictor (adj- $R^2 = 0.502$ ,  $p < 0.001$ ), with pool size adding independent variance; the final two-predictor model achieved adj- $R^2 = 0.633$ . A preliminary lagged analysis using historical CIES expatriate counts shows that the 2017 abroad count retains a Spearman correlation of +0.52 with the April 2026 FIFA ranking across thirteen European nations, consistent with a leading-indicator interpretation. Relative age effect analysis revealed a pan-European birth-month  $Q_1/Q_4$  ratio of 1.39 ( $\chi^2_{11} = 363.6$ ,  $p < 0.001$ ), with a theoretically consistent reversal in England and Wales (August academic cutoff). Mean  $FQ$  improvement of +3 points is analytically equivalent to multiplying the participating population by 1.7–2.0 $\times$ , depending on baseline distance from threshold.

**Conclusions.** The  $FQ$  framework offers national associations a quantitative basis for development strategy. Because professional output is a threshold phenomenon,

47 raising the population mean generates disproportionate returns that participation  
48 growth alone cannot match at comparable cost. The European Union's free movement  
49 of labour provides an empirical market mechanism that continuously calibrates the  
50 threshold, lending ecological validity to the model. Associations below the European  
51 mean face structural underperformance; those with high participation bases but  
52 declining registration trends face a lagged collapse risk. The framework itself and its  
53 qualitative implications — mean-shifting efficiency, the size premium, the threshold  
54 mechanism, and EU labour-market calibration — are the durable contribution; exact  
55 national point estimates are illustrative given current heterogeneity in registration  
56 data, but the ranking direction and efficiency calculations are robust within plausible  
57 adjustments to the denominators.

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# 1 Introduction

The production of professional footballers is unequally distributed across Europe in ways that resist simple explanation. France and Germany, with populations of 68 and 85 million respectively and the continent’s largest registered player bases, sit near the bottom of European nations in terms of professional players produced per active participant. Serbia (population 6.6 million) and Croatia (3.9 million) produce senior professionals at rates roughly an order of magnitude higher per active participant. Scotland, with 5.5 million people, consistently exports more players per participant than England, despite sharing a border, a language, and comparable infrastructure investment.

These disparities have attracted attention in the coaching science literature, with proposed mechanisms including relative age effects (Barnsley et al., 1985; Cobley et al., 2009; Helsen et al., 2012), talent identification methodology (Vaeyens et al., 2008), and the volume and quality of deliberate practice (Helsen et al., 1998). Informal accounts also point to differences in unstructured play culture and street football, though robust cross-national quantitative evidence on these mechanisms is limited. While each explanation carries empirical support, none provides a unified quantitative framework capable of ranking nations, estimating the magnitude of underperformance, or comparing the cost-effectiveness of competing development interventions.

This paper proposes such a framework. We introduce the *Football Quotient* ( $FQ$ ), a latent-ability construct that treats the distribution of football ability within a population as approximately normal, calibrated to the pan-European professional player conversion rate. The  $FQ$  is not claimed to be a universal psychometric measure; it is an organisational tool for national associations. Each association’s playing population has an empirically observed conversion rate to senior professional status, and that rate implies a location for the association’s ability distribution relative to the threshold at which professional employment becomes attainable. Shifting that location—raising the mean  $FQ$ —produces disproportionate increases in professional output because the relevant quantity is a tail probability.

Although the empirical focus is football, the framework developed here is not solely

128 a football paper. Professional output in any threshold-based domain depends on how  
129 much of the underlying population distribution lies above the relevant threshold. That is  
130 a general property of tail statistics, and the development investment logic that follows  
131 from it — prioritise raising the mean over expanding elite selection — applies wherever  
132 ability is distributed across a population and professional attainment is a threshold event.  
133 Football is the test case. The mechanism belongs to a broader theory of developmental  
134 investment under threshold conditions, and the paper argues it explicitly in that capacity.

135 A precedent for this style of analysis exists in the cross-country sports economics  
136 literature. [Bernard and Busse \(2004\)](#) model Olympic medal totals as a function of  
137 population and economic resources, finding that population and per-capita GDP contribute  
138 approximately equally at the margin to a country’s Olympic output. Their model rests  
139 on the explicit assumption that “athletic talent is most likely distributed normally in  
140 the world’s population” and that countries can be treated as “arbitrary divisions of the  
141 world population,” so that medal-calibre athletes appear in the upper tail of a shared  
142 underlying distribution. The framework presented here adopts the same distributional  
143 and tail-event structure but specialises it in two ways: to a single sport rather than  
144 the Olympic medal aggregate, and to a continuously calibrated professional employment  
145 threshold rather than a fixed-quota podium. Where Bernard and Busse decompose Olympic  
146 output into population and GDP per capita, we decompose football professional output  
147 into participation base and a population-mean ability parameter (the  $FQ$ ), and derive  
148 analytically how their relative marginal returns depend on distance from the threshold.  
149 The substantive contribution beyond the production-function tradition is the threshold-  
150 geometry result — that mean-shifting dominates base expansion at the margin precisely  
151 because professional employment is a tail event — together with the identification of  
152 the EU football labour market as the empirical mechanism that calibrates the threshold.  
153 The parallel with the long-term athlete development literature ([Côté and Vierimaa, 2014](#))  
154 should also be acknowledged: the prescription that follows from the framework — invest  
155 in the average quality of development rather than in earlier and more aggressive selection  
156 — aligns with the “sampling” tradition of that literature, though derived here from a

157 distributional rather than a developmental-psychology argument.

158 Three specific contributions are made:

- 159 1. We derive implied national mean  $FQ$  scores for 29 European nations from 2024/25  
160 senior professional player data and demonstrate that the resulting ranking is mean-  
161 ingfully distinct from both FIFA rankings and population size.
- 162 2. We provide an analytical result—and supporting empirical illustration—showing that  
163 mean-shifting is substantially more efficient than participation growth for generating  
164 additional professional players, and quantify this efficiency advantage as a function  
165 of a nation’s current distance from the professional threshold.
- 166 3. We identify a market mechanism—the European Union’s free movement of labour  
167 for footballers—that continuously calibrates the professional threshold in practice,  
168 providing ecological validity for a model that might otherwise appear purely theoret-  
169 ical.

170 This paper is best understood as a framework offered together with an illustrative  
171 empirical pass over the best data currently available. The mathematical structure —  
172 threshold via labour-market arbitrage, the multidimensional bundle that the threshold  
173 selects on, mean-shifting efficiency under tail probability, the nested tier structure — is the  
174 durable contribution and stands independently of how precisely any individual country’s  
175 mean  $FQ$  can be estimated today. The empirical estimates are illustrations of what the  
176 framework yields when applied to Transfermarkt-derived squad data, FIFA Big Count  
177 and federation registration figures, and CIES Football Observatory cross-checks. Each  
178 of those sources has known heterogeneity in definition, coverage, and recency. The work  
179 is therefore best read as a precursor to a coordinated UEFA-level data effort that the  
180 framework itself motivates: consistent registration definitions across federations, pan-  
181 European player-tracking with known coverage, longitudinal cohort series, and individual  
182 threshold calibration. Section 5.12 sets out that research programme in detail.

183 The remainder of the paper is structured as follows. Section 2 develops the theoretical  
184 framework, including the  $FQ$  model, the threshold mechanism, and the mean-shifting

185 efficiency result. Section 3 describes data sources and preprocessing. Section 4 presents  
186 national  $FQ$  estimates, regression models of FIFA ranking, relative age effect analysis,  
187 and size premium calculations. Section 5 discusses implications for national development  
188 strategy, structural collapse risk, and the limitations of the approach. Section 6 concludes.

## 189 2 Theoretical Framework

190 The framework that follows is a set of conditional claims. Given the assumptions stated  
191 in this section — that football ability is approximately normally distributed within an  
192 active playing population, that  $\sigma$  is comparable across nations at the scale used here, and  
193 that the European professional labour market arbitrages a continuous threshold  $T$  — the  
194 mathematical results in Sections 2.4–2.5 follow as theorems and the empirical estimates in  
195 Section 4 follow as calculations. Where any assumption fails, the consequences propagate  
196 to the conclusions in ways the sensitivity analyses in Sections 5.2 and 5.11 quantify where  
197 possible. The paper is best read as a structure offered for inspection: granting the premises  
198 gives the conclusions; rejecting a premise indicates exactly which step of the analysis the  
199 reader needs to revise.

### 200 2.1 The Football Quotient

201 We model the football ability of a randomly selected member of a nation’s active playing  
202 population as a random variable  $X \sim \mathcal{N}(\mu, \sigma^2)$ , where  $\mu$  is the nation-specific mean  
203 ability and  $\sigma = 15$  is fixed across all nations. The normal distribution is adopted as a  
204 modelling convenience, following the established psychometric convention — traceable to  
205 Quetelet’s 1835 work on human traits and Galton’s 1869 extension to natural ability — of  
206 representing individual-difference distributions in unimodal symmetric form (Simonton,  
207 1999), and motivated by its tractability for deriving closed-form efficiency comparisons.  
208 The choice of  $\sigma = 15$  mirrors the conventional Wechsler IQ scaling (Anastasi and Urbina,  
209 1997), creating an interpretable unit in which one standard deviation separates clearly  
210 distinct levels of performance. We do not claim this parameterisation is uniquely correct;

211 the qualitative results depend only on unimodality and monotone tails, properties shared  
 212 by all members of the location-scale family.

213 The  $FQ$  of an individual is their position on this scale. A national mean  $FQ$  of 100 places  
 214 a country at the European average; a mean of 106 (roughly Scotland’s estimate) means the  
 215 median active player in that country is as capable as approximately the 66th-percentile  
 216 player in an average European country.

## 217 **2.2 The Professional Threshold**

218 Professional football employment is modelled as a threshold process: a player achieves  
 219 senior professional status if and only if their ability  $X$  exceeds a threshold  $T$ . The threshold  
 220 is not fixed by regulatory fiat but by market forces: the number of professional positions  
 221 across Europe is finite, and competition for those positions determines who crosses the  
 222 threshold.

223 The pan-European conversion rate  $\bar{r}$  is defined as:

$$\bar{r} = \frac{\sum_c N_c^{\text{pro}}}{\sum_c P_c^{\text{active}}} \quad (1)$$

224 where  $N_c^{\text{pro}}$  is the number of senior professionals from nation  $c$  and  $P_c^{\text{active}}$  is the estimated  
 225 active playing population. For a country at the European mean ( $\mu = 100$ ), the threshold  
 226 satisfies:

$$\bar{r} = 1 - \Phi\left(\frac{T - 100}{15}\right) \quad (2)$$

227 which gives:

$$T = 100 + 15 \Phi^{-1}(1 - \bar{r}) \quad (3)$$

228 Given the observed pan-European rate of  $\bar{r} = 1.1747 \times 10^{-3}$ , this yields  $T = 145.6$ .

229 The threshold-truncation form of this model warrants a brief note relative to the prior  
 230 literature. [Simonton \(1999\)](#) explicitly considered and rejected a threshold-truncation  
 231 account of *creative productivity* — the proposal that the skewed distribution of creative  
 232 output reflects nothing more than the upper tail of an underlying normal ability distribution  
 233 above some minimal threshold for creative work. Simonton’s objection is that the right-

234 hand tail of the productivity distribution extends far beyond what truncation of a normal  
 235 can produce, requiring multiplicative-influence or combinatorial-explosion mechanisms to  
 236 generate the observed skew in count data. That objection does not apply to the present  
 237 framework. The *FQ* model does not predict the distribution of creative or productive  
 238 output; it predicts the binary outcome of whether an individual crosses the professional  
 239 employment threshold, which is precisely the case in which truncation of a normal ability  
 240 distribution is the appropriate model. The conversion rate  $r_c$  is a tail probability, not a  
 241 count distribution, and the mean-shifting efficiency results in Section 2.5 follow directly  
 242 from this fact. Where Simonton argues that ability-threshold models cannot account for  
 243 productive output, we are claiming only that ability exceeds a threshold or it does not.

### 244 **2.3 Implied National Mean FQ**

245 For a nation with mean *FQ*  $\mu_c$ , the conversion rate is:

$$r_c = 1 - \Phi\left(\frac{T - \mu_c}{15}\right) \quad (4)$$

246 Inverting, the implied mean *FQ* is:

$$\mu_c = T - 15 \Phi^{-1}(1 - r_c) \quad (5)$$

247 This is the central estimator used throughout the empirical analysis. Its interpretation  
 248 is straightforward: if a country produces professionals at twice the pan-European rate, its  
 249 ability distribution sits at a higher location on the *FQ* scale, and equation (5) quantifies  
 250 that location precisely.

### 251 **2.4 National Team Quality via Order Statistics**

252 A national team is drawn from the upper tail of the country's playing population  $P_c$ . Under  
 253 the *FQ* model, the expected ability of the  $k$ -th best player out of  $P_c$  is approximately

254 (Blom, 1958):

$$\mathbb{E}[X_{(k)}] \approx \mu_c + 15 \Phi^{-1}\left(1 - \frac{k}{P_c}\right) \quad (6)$$

255 The average  $FQ$  of a 30-man national squad (selecting the top 30 from the active  
256 population) is therefore:

$$\overline{FQ}_c^{\text{NT}} = \mu_c + \frac{15}{30} \sum_{k=1}^{30} \Phi^{-1}\left(1 - \frac{k}{P_c}\right) \quad (7)$$

257 Equation (7) captures the *size premium*: a country with a large active population  
258 selects its national team from a deeper pool, systematically producing a higher national  
259 team quality even when its mean  $FQ$  is below the European average. Germany, for example,  
260 has an estimated mean  $FQ$  of 96.5 but an expected national team average  $FQ$  of 162.7—a  
261 size premium of +66.2 points. This decomposition is directly relevant to development  
262 strategy, as it reveals that large-population nations are insulated from deficiencies in mean  
263 ability by pool depth, but only so long as that pool depth is maintained.

## 264 2.5 The Mean-Shifting Efficiency Result

265 Consider two interventions applied to a nation with mean  $FQ$   $\mu_c$  and active population  $P_c$ :

- 266 1. **Participation increase**: scale the active population by factor  $m > 1$ , holding the  
267 distribution shape constant. Professional output scales linearly:  $N^{\text{pro}} \mapsto m \cdot N^{\text{pro}}$ .
- 268 2. **Mean shift**: raise the mean  $FQ$  by  $\Delta$  while holding  $P_c$  constant. Professional output  
269 scales by:

$$\rho(\Delta, \mu_c) = \frac{1 - \Phi\left(\frac{T - \mu_c - \Delta}{15}\right)}{1 - \Phi\left(\frac{T - \mu_c}{15}\right)} \quad (8)$$

270 **Proposition 1.**  $\rho(\Delta, \mu_c) > 1$  for all  $\Delta > 0$ . Moreover, the equivalent participation  
271 multiplier  $m = \rho(\Delta, \mu_c)$  grows super-linearly in  $\Delta$ : a +3  $FQ$  shift requires approximately  
272 1.7–2.0× participation to match, a +6 shift requires 3.5–4.0×, and a +9 shift requires  
273 6–8×.

274 *Sketch.*  $\rho$  is the ratio of two survival probabilities of the normal distribution with the  
275 numerator evaluated at a lower  $z$ -score. Since  $\Phi$  is strictly monotone and the normal

276 survival function  $1 - \Phi(z)$  is log-convex in  $z$ , shifting  $z$  downward by  $\Delta/15$  produces a  
 277 multiplicative gain in the survival probability that grows with  $z$ . The quantitative values  
 278 follow from numerical evaluation of equation (8) at the empirical threshold  $T = 145.6$   
 279 across baseline means  $\mu_c \in [96.5, 109.0]$ . □ □

280 **Corollary 1.** *The efficiency advantage of mean-shifting is greatest for countries furthest*  
 281 *below the threshold (lowest  $\mu_c$ ), and decreases as a country approaches the threshold.*  
 282 *Germany ( $\mu_c = 96.5$ ) gains a +3 FQ shift equivalent to  $\approx 2.0\times$  participation; Serbia*  
 283 *( $\mu_c = 109.0$ ) gains only  $\approx 1.7\times$  equivalent.*

284 This corollary has a counterintuitive implication: the development efficiency argu-  
 285 ment for mean-shifting is strongest precisely for countries conventionally regarded as  
 286 underperforming—those with low mean  $FQ$ . However, in absolute terms, the *cost* of  
 287 achieving a given mean shift may differ greatly between nations. Section 5 addresses this  
 288 distinction.

289 Figure 1 illustrates the key result. The left panel shows normal distribution curves at  
 290 baseline and three shifted means, with the professional threshold marked. Even modest  
 291 rightward shifts visibly increase the shaded tail above the threshold. The right panel  
 292 plots the professional output multiplier as a function of mean shift for three representative  
 293 national baselines, demonstrating the super-linear advantage over equivalent participation  
 294 investment.

### Mean-shifting vs Participation Increase: Effect on Professional Output

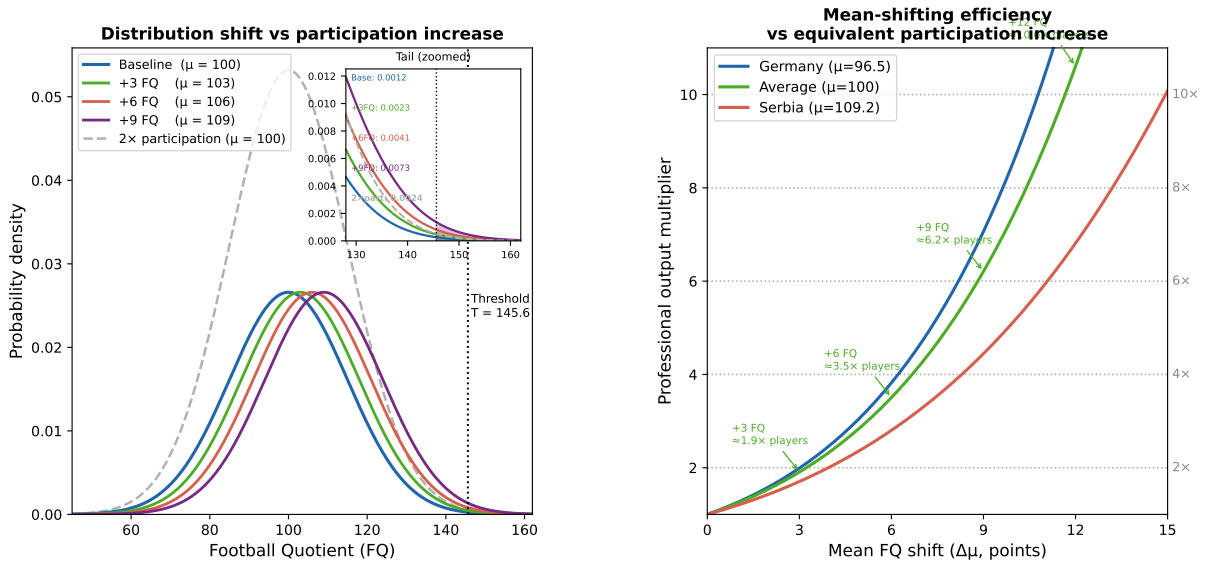


Figure 1: **Mean-shifting versus participation increase.** *Left:* Normal distribution curves for baseline ( $\mu = 100$ ) and three mean-shifted scenarios, with the pan-European professional threshold ( $T = 145.6$ ) marked. The inset zooms the tail above threshold; numerical tail probabilities are annotated. The dashed curve represents a 2 $\times$  participation increase (same distribution, scaled population). *Right:* Professional output multiplier as a function of mean  $FQ$  shift  $\Delta\mu$  for three national baselines representative of Germany (low mean, large pool), the European average, and Serbia (high mean, small pool). Horizontal reference lines indicate equivalent participation multipliers. A +6 FQ shift achieves what a 3.5 $\times$  participation increase achieves for the average nation.

## 295 2.6 The European Labour Market as Threshold Calibrator

296 A potential objection to the threshold model is that professional employment levels are  
 297 institutionally determined—leagues have fixed squad sizes—rather than arising from a  
 298 continuous ability market. This objection would be decisive if players competed only  
 299 within their national borders. The European Union’s free movement of labour, combined  
 300 with the longstanding Bosman ruling (Court of Justice of the European Union, 1995),  
 301 creates instead a continental labour market in which players arbitrage across leagues.<sup>1</sup> A  
 302 player with  $FQ$  above 145.6 who cannot secure a domestic contract can and routinely does  
 303 obtain employment in a league where the threshold is locally lower.

<sup>1</sup>The continental labour market for footballers in fact rests on more than the *Bosman* ruling alone. The Court of Justice subsequently extended non-discrimination protections to nationals of countries holding Association Agreements with the EU (Court of Justice of the European Union, 2003, 2005), and successive EU enlargements (2004, 2007, 2013) brought additional national pools into the freedom-of-movement regime. The cumulative effect is a substantially larger labour market than *Bosman* alone defined.

304 The empirical evidence for this mechanism is clear: our dataset records 73% of French  
305 senior professionals playing abroad, 56% of Croatian professionals, and 56% of Welsh  
306 professionals. The cross-border flow is not random but ability-sorted: players migrate to  
307 leagues whose quality level matches their ability. This continuous arbitrage ensures that  
308 the threshold  $T$  is not a modelling artefact but a real economic quantity—the minimum  
309 ability level required to obtain and sustain professional employment somewhere in the  
310 European professional ecosystem.

311 What  $FQ$  measures, accordingly, is not football skill in a narrow technical sense but  
312 the bundle of attributes required to obtain and sustain professional employment in this  
313 market. That bundle includes technical and physical ability, but it also includes the  
314 psychological and lifestyle factors long recognised in the talent-development literature:  
315 willingness to relocate, tolerance of competitive pressure and contract instability, disci-  
316 pline around training and recovery in low-supervision environments, and resilience under  
317 repeated rejection. The threshold is therefore defined functionally—by who clears it,  
318 through whatever combination of route and bundle works—rather than by any specific  
319 developmental pathway. Players reach professional status through many imperfect routes;  
320 the threshold is path-invariant because it is set by the labour market that sits downstream  
321 of all of them.

322 The implication is that a national association need not achieve a globally valid normal  
323 distribution of ability. It need only shift its distribution rightward relative to the threshold—  
324 raising the share of its population that can compete in the continental labour market. The  
325 normality assumption is a tractable parameterisation of this monotone relationship; the  
326 policy conclusion holds under any unimodal distribution.

### 327 **The professional threshold as an instance of a nested structure**

328 The threshold model developed here is the professional instance of a more general nested-  
329 threshold structure. Every organised tier of football—local recreational leagues, district  
330 divisions, regional and semi-professional tiers, lower professional divisions, top-flight,  
331 and the elite continental level—operates as a labour market for that tier, with its own

332 functional threshold and its own conversion rate from the tier below. The mean-shifting  
333 result therefore applies at each tier, not only at the professional one; densification of the  
334 lower tiers is the mechanism through which the professional tail thickens. This paper  
335 concerns the professional threshold because that is where data are most readily collected,  
336 but the framework generalises downward, and most of the developmental investment  
337 implications discussed in Section 5 act through the lower tiers rather than directly on the  
338 professional cutoff.

## 339 **3 Data and Methods**

### 340 **3.1 Professional Player Counts**

341 Senior professional player counts were obtained from two sources. First, club squad data for  
342 2024/25 was collected from Transfermarkt (<https://www.transfermarkt.co.uk>) for all  
343 professional leagues in 29 European nations, covering both top-flight and lower professional  
344 tiers. Player nationality was taken from the primary nationality recorded by Transfermarkt,  
345 which reflects the player’s principal national association affiliation. Second, for leagues not  
346 included in the publicly available dcaribou (dcaribou, 2024) dataset—comprising second  
347 and lower tiers in 23 nations—squad pages were scraped directly using standard HTTP  
348 requests with rate limiting ( $\geq 1.5$  s between requests).

349 To obtain a consistent definition of *professional*, we applied a **senior-only filter**: only  
350 players born in 2003 or earlier (age  $\geq 21$  in the 2024/25 season) were counted. This  
351 threshold excludes academy and development-squad players who hold nominal professional  
352 contracts but have not yet demonstrated sustained professional-level performance. The  
353 cut-off is consistent with UEFA and domestic federation definitions of senior professional  
354 status and removes the confounding inflation that arises from extended squad lists (/plus/1  
355 pages on Transfermarkt) which include youth development players.

356 Players appearing in multiple competitions within the same country (for example,  
357 an Irish player appearing in both League of Ireland divisions) were deduplicated by  
358 Transfermarkt player ID before counting, ensuring each individual is counted once toward

359 their nation’s domestic total.

360 For nationals playing abroad, counts were cross-validated against CIES Football  
361 Observatory monthly reports (CIES Football Observatory, 2024). Where CIES reported  
362 higher abroad counts than Transfermarkt (indicating coverage gaps in the scraped data),  
363 the CIES figure was used as a lower bound override.

### 364 **3.2 Registered and Active Player Counts**

365 Registered player totals were compiled from the FIFA Big Count survey (Fédération  
366 Internationale de Football Association, 2007) as the primary baseline, updated with the  
367 most recent federation-level reports where available. The relevant active population for  
368 conversion rate purposes excludes registered players who are inactive, administrative, or  
369 referee-affiliated, and excludes female players and players under 16.

370 A *conflation correction* was applied for nations where the FIFA Big Count registration  
371 definition includes all registered individuals regardless of activity level. The correction  
372 replaces the FIFA Big Count number with a federation-published active-player figure for  
373 those nations where the two disagree materially.<sup>2</sup> Countries were assigned a registration  
374 confidence level (HIGH / MED / LOW) based on source recency and specificity.

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<sup>2</sup>The size of the correction varies by federation and reflects what each association reported to FIFA in 2006. The Deutscher Fußball-Bund’s submission of 6.29M *Vereinsmitglieder* (club members) is the largest documented case: cross-referenced against the DFB *Jahresbericht* 2006, the count of active competitive licence holders was approximately 1.73M, giving an active/total ratio of  $\sim 0.28$ . The English FA’s submission included recreational and Respect-programme affiliates in addition to competitive players; the FA Active People Survey 2005–07 indicates approximately 1.1M regular competitive players against the 1.53M reported figure (ratio  $\sim 0.72$ ). The Italian FIGC’s submission included non-playing administrative *tesserati*; the FIGC *Rapporto Calcio* 2006 reports 1.4M active *tesserati* against 1.696M total (ratio  $\sim 0.83$ ). Smaller corrections were applied to France (FFF *Rapport Annuel*,  $\sim 0.91$ ) and Spain (RFEF *Memoria*,  $\sim 0.96$ ). Federations whose reporting matched their active competitive register — including the Croatian, Scottish, Welsh, and Nordic associations — received no adjustment. The full per-country adjustment factor and source citation is in the supplementary data file `registered_base.csv`.

Table 1: **Data coverage summary.** Leagues covered, total clubs, and player count before and after senior filter, by source.

Source	Nations	Leagues	Senior pros (post-filter)
dcaribou (StatsBomb open data)	29	29	13,407
Transfermarkt scraped (domestic)	23	57	5,132
CIES abroad override	8	—	1,110
Total (deduplicated)	29	86	19,649

### 3.3 FQ Calculation

The pan-European conversion rate was computed as total senior professionals divided by the sum of estimated active players across all 29 nations ( $\bar{r} = 1.1747 \times 10^{-3}$ ). The professional threshold was derived from equation (3), giving  $T = 145.6$ . National implied means were computed from equation (5) using each nation’s conversion rate  $r_c$ .

### 3.4 Confidence Intervals

Registration totals are known with varying precision. To propagate this uncertainty into  $FQ$  estimates, we conducted a Monte Carlo simulation ( $n = 10,000$  iterations) in which registered player counts were drawn from log-normal distributions. The log-normal coefficient of variation (CV) was set according to confidence level: HIGH (CV = 0.05), MED (CV = 0.12), LOW (CV = 0.20). Professional player counts were simultaneously perturbed by  $\pm 10\%$  uniform noise to reflect coverage uncertainty. The 2.5th and 97.5th percentiles of the resulting  $FQ$  distribution define the reported 95% confidence intervals.

### 3.5 Regression Models

To assess the relationship between the  $FQ$  framework measures and competitive outcome, FIFA world rankings (April 2026) were regressed on combinations of: (1) log-transformed active pool size, (2) log-transformed abroad professional count, and (3) implied mean  $FQ$ . Six nested models were estimated using OLS with robust standard errors. Spearman partial

393 correlations controlling for log pool size were computed to assess directional relationships  
394 without distributional assumptions. Variance inflation factors (VIF) were computed for  
395 collinearity diagnostics.

### 396 **3.6 Relative Age Effect Analysis**

397 Date of birth (day, month, year) was extracted for all senior professionals with available  
398 data ( $n = 20,197$ ). Birth months were tabulated and compared against a uniform expected  
399 distribution scaled to the number of days in each month. An overall  $\chi^2$  test ( $df = 11$ ) was  
400 conducted, followed by per-country  $\chi^2$  tests. The  $Q_1/Q_4$  ratio (January–March versus  
401 October–December) was used as a summary statistic. For England and Wales, the analysis  
402 was repeated using an August academic year cutoff ( $Q'_1 = \text{August–October}$ ,  $Q'_4 = \text{May–}$   
403  $\text{July}$ ) to reflect the known reversal of relative age effects under different institutional cutoff  
404 dates (Helsen et al., 2000; Musch and Grondin, 2001).

## 405 **4 Results**

### 406 **4.1 National FQ Estimates**

407 Table 2 presents the full results for all 29 nations. The pan-European conversion rate of  
408 1.17 per 1,000 active players implies a professional threshold of  $T = 145.6$ —approximately  
409 3 standard deviations above the European mean ability.

Table 2: **National Football Quotient estimates, 2024/25.** Countries ranked by implied mean  $FQ$ . CI = 95% Monte Carlo confidence interval. NT Avg = expected national team average  $FQ$  (top-30 order statistic). Abroad% = proportion of senior professionals based outside home country. Conf. = registration confidence level. The Pan-European row reports the aggregate active pool and senior professional count; the listed mean  $FQ$  of 100 is by calibration construction (see equation 3) rather than a population-weighted average of the country estimates.

Country	Active pool	Total pros	Abroad (abs.)	Abroad (%)	Mean $FQ$	CI (95%)	NT Avg	FIFA Rank	Conf.
Serbia	120,194	878	392	44.6	109.0	[105.9–112.6]	164.9	39	LOW
Croatia	118,316	697	392	56.2	107.9	[105.3–110.8]	163.5	11	LOW
Scotland	161,412	747	190	25.4	106.6	[105.3–107.6]	163.4	43	HIGH
Slovenia	60,334	216	99	45.8	105.3	[103.7–106.8]	158.3	58	MED
Slovakia	90,000	282	119	42.2	104.6	[102.5–106.8]	159.2	48	LOW
Wales	105,603	306	170	55.6	104.2	[103.0–105.2]	159.4	37	HIGH
Portugal	235,000	665	363	54.6	104.1	[102.8–105.3]	162.3	5	HIGH
Ireland	220,000	471	217	46.1	102.7	[101.6–103.7]	160.7	59	HIGH
Bulgaria	120,000	236	46	19.5	102.4	[100.4–104.5]	158.1	86	LOW
Romania	300,000	567	67	11.8	102.2	[100.5–103.9]	161.3	56	MED
Austria	248,000	447	131	29.3	102.0	[100.5–103.4]	160.4	24	MED
Sweden	379,681	649	265	40.8	101.7	[100.6–102.6]	161.7	38	HIGH
England	1,400,000	2,169	586	27.0	101.3	[100.2–102.2]	165.7	4	HIGH
Finland	150,894	231	71	30.7	101.2	[100.1–102.1]	157.7	73	HIGH
Czech Rep.	358,000	535	84	15.7	101.1	[ 99.6–102.5]	160.8	41	MED
Italy	1,131,906	1,689	165	9.8	101.1	[ 99.9–102.0]	164.8	12	HIGH
Denmark	381,840	534	269	50.4	100.8	[ 99.7–101.7]	160.7	20	HIGH
Belgium	400,000	529	294	55.6	100.5	[ 99.4–101.5]	160.6	9	HIGH
Norway	413,139	513	161	31.4	100.2	[ 99.1–101.2]	160.4	31	HIGH
Switzerland	273,644	334	114	34.1	100.1	[ 98.7–101.5]	158.9	19	MED
Greece	200,000	197	86	43.7	99.2	[ 97.6–100.8]	156.8	47	MED
Spain	1,248,511	1,146	451	39.4	98.9	[ 97.8– 99.8]	162.9	2	HIGH
Ukraine	1,016,000	810	204	25.2	98.3	[ 96.4–100.2]	161.6	32	LOW
Hungary	300,000	239	68	28.5	98.2	[ 97.2– 99.1]	157.3	42	HIGH
France	2,060,960	1,494	1091	73.0	97.8	[ 96.8– 98.7]	163.5	1	HIGH
Poland	769,000	536	112	20.9	97.7	[ 95.9– 99.6]	160.1	35	LOW
Netherlands	1,100,000	714	367	51.4	97.4	[ 96.3– 98.2]	160.9	7	HIGH

410 The range of implied mean  $FQ$  scores spans 12.5 points, from Serbia (109.0) to Germany  
411 (96.5). This span, while appearing modest on the  $\mathcal{N}(100, 15^2)$  scale, translates to large  
412 differences in tail probability: a country at  $\mu = 109$  produces professionals at roughly  $14\times$   
413 the rate of a country at  $\mu = 96.5$ , given the same active population.

414 Several features of Table 2 are noteworthy:

- 415 • **FIFA ranking and mean  $FQ$  are weakly correlated.** France (FIFA rank 1) has  
416 a mean  $FQ$  of 97.8, below the European average. Germany (FIFA rank 10) sits at  
417 96.5, the lowest estimate in the dataset. These nations compensate for below-average  
418 ability distributions with exceptional pool depth (size premium of +66 and +66  $FQ$   
419 points, respectively; see Section 4.3).
- 420 • **Small nations at the top of the  $FQ$  ranking convert at multiples of the  
421 European average.** Serbia (7.3 per 1,000,  $6.2\times$  the European mean), Croatia  
422 (5.9 per 1,000,  $5.0\times$ ), and Scotland (4.6 per 1,000,  $3.9\times$ ) achieve this without large  
423 absolute populations, indicating genuine distributional advantages rather than simple  
424 scale effects.
- 425 • **Abroad percentage varies widely.** France (73%), Wales (55.6%), Croatia (56.2%),  
426 and Belgium (55.6%) export the highest fractions of their professionals, consistent  
427 with the EU labour market arbitrage mechanism described in Section 2. Turkey  
428 (9%) and Romania (11.8%) show low abroad percentages, suggesting either lower  
429 international labour mobility or systematic undercounting of abroad professionals.

## 430 4.2 Regression Models of FIFA Ranking

431 Table 3 presents six nested OLS models predicting FIFA ranking (April 2026). The  
432 dependent variable is coded as  $-\text{rank}$  so that higher values represent better rankings,  
433 enabling positive coefficients to indicate beneficial predictors.

Table 3: **OLS regression results: predictors of FIFA ranking** ( $n = 29$ ). Dependent variable:  $-$ FIFA rank (higher = better). Robust standard errors. \*  $p < 0.05$ , \*\*  $p < 0.01$ , \*\*\*  $p < 0.001$ .

Predictor	Model			
	(1)	(2)	(3)	(4)
Constant	$-216.9^{***}$	$-136.5^{***}$	$-701.8^{**}$	$-227.8^{***}$
log(active pool)	$14.5^{***}$	—	$23.6^{***}$	$9.2^{**}$
log(abroad count)	—	$20.2^{***}$	—	$15.1^{***}$
Mean $FQ$	—	—	$3.6^*$	—
$R^2$	0.427	0.520	0.541	0.659
adj- $R^2$	0.405	0.502	0.506	0.633

Model 5 (full): mean $FQ$ + pool + abroad				
	$\hat{\beta}$	SE	$t$	$p$
Constant	$-248.3$	230.0	$-1.08$	0.291
Mean $FQ$	0.2	1.7	0.09	0.929
log(active pool)	9.7	6.2	1.56	0.130
log(abroad count)	14.8	5.0	2.94	0.007**
adj- $R^2$	0.618; VIF: mean $FQ$ 4.6, log(pool) 5.8, log(abroad) 2.3			

434 The key results are:

- 435 1. Abroad count is the strongest single predictor of FIFA ranking (Model 2, adj-  
436  $R^2 = 0.502$ ), outperforming pool size (adj- $R^2 = 0.405$ ).
- 437 2. Pool size and abroad count together explain 63% of variance in FIFA ranking (Model  
438 4, adj- $R^2 = 0.633$ ). Both predictors remain significant ( $p < 0.01$ ,  $p < 0.001$ ) with no  
439 severe collinearity (VIF  $< 6$ ).
- 440 3. When mean  $FQ$  is added to pool and abroad count (Model 5), it becomes entirely  
441 non-significant ( $p = 0.929$ ). Mean  $FQ$  information is fully absorbed into the abroad

442 count, which is its primary manifestation: countries with high mean  $FQ$  produce  
443 more professionals per capita who then compete in higher-quality foreign leagues.

444 4. Spearman partial correlation of abroad count controlling for log pool size:  $\rho = +0.68$ ,  
445  $p < 0.001$ . For mean  $FQ$  controlling for pool size:  $\rho = +0.37$ ,  $p = 0.051$  (borderline).

446 These results suggest that FIFA ranking is primarily a function of a country's ability  
447 to produce and export internationally competitive players, rather than a simple function  
448 of population size. The mean  $FQ$  framework captures the underlying mechanism, but the  
449 most tractable observable proxy is the abroad count.

450 Figure 2 visualises the joint relationship between mean  $FQ$ , FIFA ranking, pool size,  
451 and abroad percentage across all 29 nations. The pattern is consistent with the regression  
452 results: large-pool nations (large bubbles) cluster in the upper-left quadrant (low  $FQ$ ,  
453 high FIFA ranking), while high- $FQ$  small nations occupy the right side with lower FIFA  
454 rankings but high per-capita conversion rates.

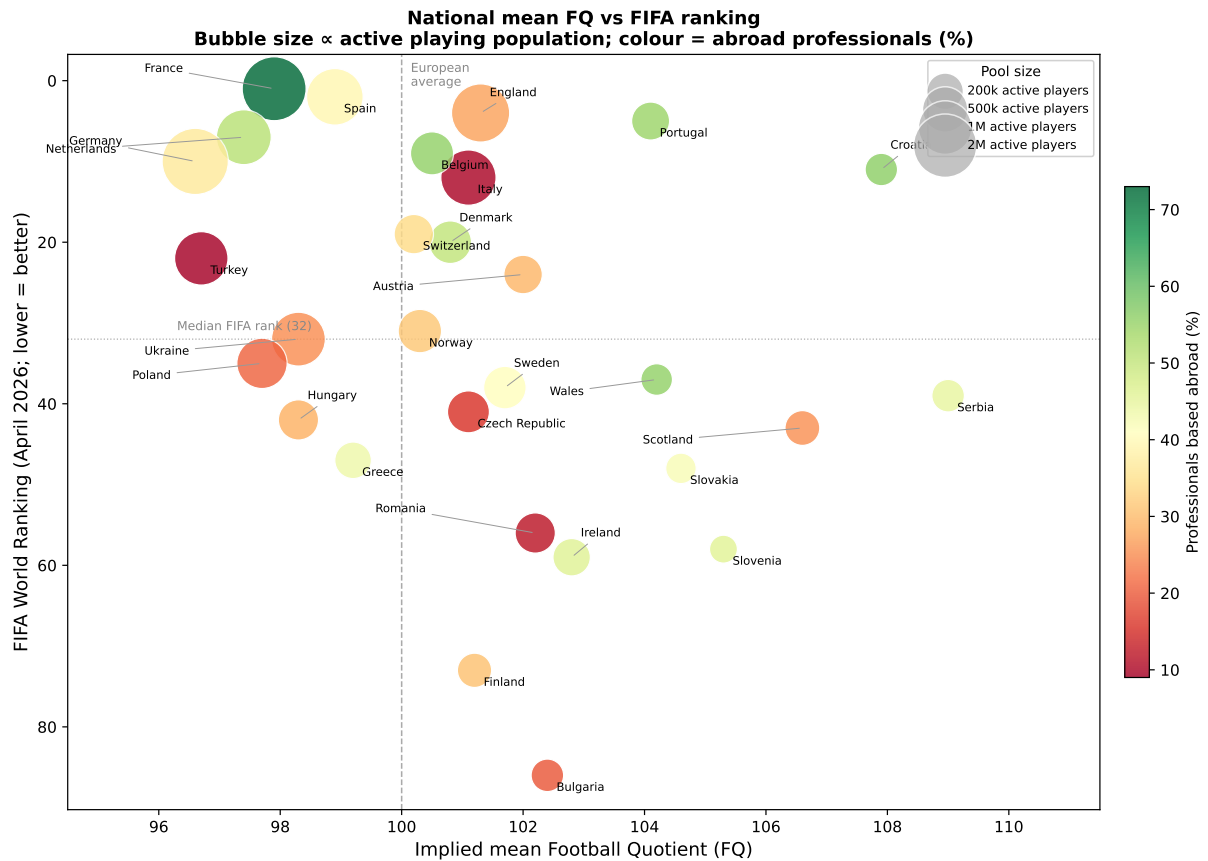


Figure 2: **National mean FQ versus FIFA world ranking.** Bubble size is proportional to the square root of the active playing population. Colour indicates the proportion of senior professionals based abroad. The vertical dashed line marks the European mean (FQ = 100); the horizontal dotted line marks the median FIFA ranking in the sample. Large-pool nations (large bubbles) achieve high FIFA rankings despite below-average mean FQ via the size premium. High-FQ small nations (right side) produce professionals at high per-capita rates but rank lower due to limited pool depth.

### 455 4.3 The Size Premium

456 Table 4 presents the decomposition of expected national team quality into mean  $FQ$  and  
 457 size premium for selected nations.

Table 4: **Size premium decomposition** for selected nations. Mean  $FQ$ : implied population mean. NT Avg: expected national team average (equation 7). Premium = NT Avg – Mean  $FQ$ .

Country	Active pool	Mean $FQ$	NT Avg	Premium	FIFA Rank
England	1,400,000	101.3	165.7	+64.4	4
Germany	2,380,000	96.5	162.7	+66.2	10
France	2,060,960	97.8	163.5	+65.7	1
Italy	1,131,906	101.1	164.8	+63.7	12
Spain	1,248,511	98.9	162.9	+64.0	2
Portugal	235,000	104.1	162.3	+58.2	5
Serbia	120,194	109.0	164.9	+55.9	39
Croatia	118,316	107.9	163.5	+55.6	11
Scotland	161,412	106.6	163.4	+56.8	43
Slovenia	60,334	105.3	158.3	+53.0	58

458 The size premium analysis reveals why large nations dominate FIFA rankings despite  
459 below-average mean  $FQ$ . Germany’s +66.2 point premium means its national team draws  
460 talent from the extreme right tail of a large population; even if the underlying mean is  
461 3.5 points below Serbia’s, the expected national team quality is comparable because the  
462 deeper pool compensates. Serbia’s +55.9 premium—achieved with only 120,000 active  
463 players—reflects the remarkable tail selection available even from a small but high-mean  
464 population.

465 Portugal exemplifies the intermediate case: a mean  $FQ$  of 104.1 combined with a  
466 moderate active pool of 235,000 yields an expected national team quality of 162.3, broadly  
467 comparable to France (163.5 expected) despite a pool 9× smaller. Portugal’s consistent  
468 placement among the world’s top five nations is well explained by this combination.

#### 469 4.4 Relative Age Effect

470 Table 5 presents birth month distributions for senior professionals in the dataset.

Table 5: **Pan-European birth month distribution** ( $n = 20,197$  senior professionals). RAE Index = observed / expected (uniform). Q1 = January–March; Q4 = October–December.

Month	Count	Expected	RAE Index
January	2,120	1,683	1.26
February	1,871	1,683	1.11
March	1,937	1,683	1.15
April	1,781	1,683	1.06
May	1,757	1,683	1.04
June	1,544	1,683	0.92
July	1,707	1,683	1.01
August	1,511	1,683	0.90
September	1,711	1,683	1.02
October	1,596	1,683	0.95
November	1,318	1,683	0.78
December	1,344	1,683	0.80

$\chi^2(11) = 363.6, p < 0.001; Q1/Q4 \text{ ratio} = 1.39$

<sup>471</sup> Table 6 presents per-country Q1/Q4 ratios under the calendar-year quarter definition.

<sup>472</sup> The pattern across countries is referenced throughout Sections 4.4 and 5.4.

Table 6: **National Q1/Q4 birth-month ratios for senior professionals.** Q1 = January–March; Q4 = October–December. Sorted by ratio descending under calendar-year quarters. England and Wales appear at the bottom because their September-1st academic cutoff inverts the calendar-year pattern; the August-cutoff-adjusted ratios for these two nations reverse direction (England 1.42<sup>\*\*\*</sup>, Wales 1.38<sup>\*\*\*</sup>; see Section 4.4). Significance: \*  $p < 0.05$ ; \*\*  $p < 0.01$ ; \*\*\*  $p < 0.001$  ( $\chi^2$  test against uniform birth-month expectation).

Country	$n$	Q1	Q4	Q1/Q4
Czech Republic	595	170	80	2.13 <sup>***</sup>
Germany	1,116	370	176	2.10 <sup>***</sup>
Spain	1,073	350	177	1.98 <sup>***</sup>
Turkey	606	204	108	1.89 <sup>***</sup>
Italy	1,900	649	347	1.87 <sup>***</sup>
Portugal	562	181	98	1.85 <sup>***</sup>
Belgium	420	138	76	1.82 <sup>*</sup>
Finland	242	77	43	1.79 <sup>**</sup>
Ukraine	807	249	140	1.78 <sup>***</sup>
Switzerland	364	128	72	1.78 <sup>**</sup>
Austria	471	141	82	1.72 <sup>**</sup>
Netherlands	651	203	121	1.68 <sup>**</sup>
Serbia	715	201	123	1.63 <sup>***</sup>
Poland	585	180	114	1.58 <sup>**</sup>
Denmark	512	159	102	1.56 <sup>***</sup>
Romania	617	175	113	1.55 <sup>**</sup>
Norway	548	148	96	1.54 <sup>***</sup>
Croatia	555	164	109	1.50 <sup>*</sup>
France	929	271	184	1.47 <sup>**</sup>
Scotland	853	262	181	1.45 <sup>*</sup>
Slovenia	225	73	53	1.38
Sweden	651	168	133	1.26 <sup>**</sup>
Ireland	603	175	139	1.26 <sup>*</sup>
Hungary	247	66	53	1.25
Slovakia	286	73	59	1.24
Bulgaria	261	73	60	1.22
Greece	200	51	26 <sup>42</sup>	1.21 <sup>*</sup>

*Inverted under calendar-year quarters (September academic cutoff):*

473 The pan-European Q1/Q4 ratio of 1.39 confirms a systematic early-birth advantage:  
474 players born in January are 26% overrepresented relative to uniform expectation, while  
475 November-born players are underrepresented by 22%. At the country level, the effect  
476 is strongest in nations with well-established youth academy systems and January 1st  
477 age-group cutoffs: Czech Republic (Q1/Q4 = 2.13\*\*\*,  $p < 0.001$ ), Germany (2.10\*\*\*),  
478 Spain (1.98\*\*\*), Turkey (1.89\*\*\*), and Italy (1.87\*\*\*).

479 The theoretically predicted reversal is observed in England (Q1/Q4 = 0.71 under  
480 calendar-year quarters; adjusted August-cutoff Q1/Q4 = 1.42\*\*\*) and Wales (0.67; adjusted  
481 1.38\*\*\*), where the September 1st academic cutoff means that players born in August and  
482 September are relatively older within their cohort and thus disproportionately selected  
483 into elite development pathways.

484 The RAE finding has a direct relationship to the  $FQ$  framework. The pan-European  
485 Q1/Q4 ratio of 1.39 implies roughly 1,800 “displaced” professionals across the dataset  
486 — around 9% of the total — whose presence in or absence from the professional pool is  
487 more plausibly explained by birth-month-driven selection than by ability. To the extent  
488 this displacement holds, the professional threshold is an imperfect sorter of underlying  
489 ability. Debiasing talent identification to remove relative age effects would improve the  
490 signal quality of the professional conversion rate as an ability indicator, and would likely  
491 shift implied mean  $FQ$  estimates upward for nations with the strongest RAE (particularly  
492 Germany, Czech Republic, and Spain).

## 493 5 Discussion

### 494 5.1 Interpreting the $FQ$ Ranking

495 The implied mean  $FQ$  ranking differs substantially from both population size and FIFA  
496 ranking. This distinction is informative in both directions. Serbia, ranking first in mean  
497  $FQ$  (109.0), is ranked 39th by FIFA; its exceptional professional conversion rate is not  
498 fully rewarded in FIFA points because its national team selection draws from a small  
499 pool, limiting the size premium available. Croatia (mean  $FQ$  107.9, FIFA rank 11) has a

500 comparable ability distribution to Serbia but produces a stronger FIFA ranking in part  
501 because its abroad players are more concentrated in high-quality leagues where FIFA  
502 ranking points are contested more frequently.

503 At the other extreme, Germany’s mean  $FQ$  of 96.5 places it last in the European  
504 ranking, yet it is consistently among the world’s top ten nations. This is largely explained  
505 by the size premium: Germany’s 2.38 million active players provide an enormous selection  
506 base from which the most extreme-right tail of the ability distribution is drawn for national  
507 team purposes.

508 The implication is that the mean  $FQ$  ranking is more informative about *developmental*  
509 *efficiency*—the quality of what a nation produces per capita— than about national team  
510 success, which depends additionally on pool depth. Both dimensions matter, but they  
511 respond to different interventions.

512 The framework also provides a unifying lens on patterns that the existing explanations  
513 cited in Section 2’s introduction account for only piecemeal. Cultural and unstructured-  
514 play accounts can describe the Serbia–Croatia outlier pattern but cannot derive the size  
515 premium, and so have nothing to say about why Germany and France remain top FIFA  
516 performers despite low mean conversion rates. Talent-identification critiques (Vaeyens  
517 et al., 2008) and the relative-age literature (Cobley et al., 2009; Helsen et al., 2012)  
518 explain why early selection systems mis-rank players within a cohort, but do not explain  
519 why aggregate professional output varies between national populations of similar size.  
520 The deliberate-practice tradition (Helsen et al., 1998) explains why individuals reach  
521 professional status but not why the rate at which a population produces them differs by  
522 an order of magnitude across European federations. The  $FQ$  framework absorbs each of  
523 these as a partial mechanism: cultural and developmental factors shape the population  
524 mean, RAE and selection bias degrade the threshold’s accuracy as an ability sorter, and  
525 deliberate practice acts as a tail-amplifier conditional on baseline ability. None of the prior  
526 mechanisms, taken individually, is contradicted; what the framework adds is the threshold-  
527 geometry result that converts these qualitative inputs into quantitative predictions about  
528 national output.

## 5.2 Confronting the Serbia Paradox: Robustness of the Headline

### Result

The most striking single result in Table 2 is also the most data-fragile: Serbia ranks first in implied mean  $FQ$  (109.0) while simultaneously carrying the widest confidence interval (95% CI 105.9–112.6) and the only *LOW* confidence registration rating among the top six nations. A reviewer encountering this will immediately ask whether the headline result is a genuine finding or an artefact of a poorly measured denominator. The question deserves a direct answer rather than a footnote.

Table 7 presents a sensitivity analysis holding Serbia’s professional count constant and varying the active player denominator across the full plausible range.

Table 7: **Serbia FQ sensitivity to registration assumption.** Professional count held fixed at 878 throughout (abroad count of 392 is CIES-validated; domestic count of 486 is Transfermarkt-sourced). Comparator FQ values: Croatia 107.9, Scotland 106.6, Portugal 104.1.

Scenario	Active players	Rate (per 1,000)	Implied FQ
Current estimate (LOW conf.)	120,194	7.30	109.0
1.5× current estimate	180,291	4.87	106.8
All registered treated as active	250,000	3.51	105.2
2.0× current estimate	240,388	3.65	105.4
2.5× current estimate	300,485	2.92	104.3

Three observations follow from this analysis.

First, Serbia’s implied FQ remains above the European average (100) and above Ireland, England, and Germany under every scenario including the extreme case of 2.5× the current active estimate. Even in that extreme case Serbia (FQ 104.3) sits effectively tied with Portugal and ahead of every larger nation in the dataset. The qualitative result — Serbia in the leading group of high-conversion nations — requires an active-population undercount of more than 2.5× to overturn, against a Monte Carlo confidence band that captures variation of less than half that magnitude.

547 Second, the direction of likely error is not obvious. Serbia’s current active estimate  
548 (120,194) represents 1.8% of its population, compared with Croatia’s 3.0% — and Croatia  
549 also carries a LOW confidence rating and sits second in the FQ ranking. If both countries  
550 are measured on comparable methodology, as is likely given their shared governance  
551 context, the denominator uncertainty affects them similarly and their relative positions  
552 are more stable than the individual confidence intervals suggest. Applying Croatia’s  
553 participation rate to Serbia’s population would yield approximately 201,000 active players,  
554 implying a Serbian FQ of  $\sim 106.5$  — still third highest in the dataset, behind only Croatia.

555 Third, the professional count itself provides a partial internal check. Serbia’s abroad  
556 total of 392 professionals is cross-validated against the CIES Football Observatory and is  
557 the more reliable half of the estimate. Even using only the abroad count as a conservative  
558 lower bound on Serbian professional output, the implied FQ is 104.8 — above Portugal,  
559 Ireland, and all larger nations.

560 The conclusion is that Serbia’s top ranking is robust to the plausible range of registration  
561 uncertainty. The LOW confidence rating reflects genuine data quality limitations and  
562 should temper exact point comparisons, as the confidence intervals reflect. It does not,  
563 however, constitute grounds for dismissing the result: the sensitivity analysis shows that  
564 Serbia would need a registration undercount of implausible magnitude, or a simultaneous  
565 overcount of professional numbers, to fall below the top four. The headline finding survives  
566 scrutiny.

567 The same logic generalises beyond Serbia to the high-FQ group as a whole. The  
568 qualitative pattern at issue — that small high-conversion nations (Serbia, Croatia, Ice-  
569 land, Scotland, Portugal) cluster above large low-conversion nations (Germany, France,  
570 Netherlands) — is observable in raw professional counts per 1,000 active players *before*  
571 *any modelling*, and is therefore not an artefact of the FQ transformation. Overturning the  
572 leading group requires more than adjusting any single nation’s denominator: it requires  
573 simultaneous upward adjustments of  $>2\times$  to the active-player denominators of multiple  
574 small nations *and* simultaneous downward adjustments to those of multiple large nations.  
575 No plausible registration heterogeneity story produces this pattern, since the federation-

576 reporting practices that inflate denominators (broad inclusion of grassroots participants)  
577 operate in the same direction across countries with comparable governance structures.  
578 The robustness of the top group is therefore stronger than the robustness of any single  
579 nation’s position within it.

### 580 **5.3 Development Strategy: Small and Large Nations**

581 The mean-shifting efficiency result (Section 2.5) has asymmetric implications for small  
582 and large nations.

583 **Small nations** face a binding constraint on participation growth: doubling the active  
584 population of Slovenia from 60,000 to 120,000 is not trivially achievable and would likely  
585 require generational effort. However, the same investment directed at raising the quality  
586 of coaching, methodology, and development environment—shifting the mean  $FQ$  by +3  
587 points—delivers an output multiplier of approximately  $1.79\times$  (per equation 8 at  $\mu_c = 105.3$ ).  
588 This is close to, though slightly below, what a literal  $2\times$  participation increase would  
589 produce, and it is a far more achievable intervention in a country whose participation  
590 base is already constrained by population. For a small nation already above the European  
591 mean, the marginal return to mean-shifting remains substantial.

592 **Large nations** are less dependent on mean-shifting because their size premium provides  
593 a buffer. Germany at  $\mu_c = 96.5$  already fields a competitive national team from its right tail.  
594 However, the model identifies a structural vulnerability: the size premium is only available  
595 while pool depth is maintained. If registered player numbers decline, the national team  
596 quality degrades with a lag of 15–20 years (the time for the current youth population to  
597 age through to senior professional status). Italy has experienced the most widely reported  
598 registration decline: the 2006 FIFA Big Count recorded 1.70M registered Italian players,  
599 against current FIGC active figures of 1.13M — a nominal decline of  $-33.3\%$ , although  
600 the two figures use different definitional bases and the precise magnitude should be treated  
601 as indicative rather than exact. Germany’s active player count has also fallen substantially  
602 since the FIFA Big Count baseline. Under the order-statistics model, sustained registration  
603 declines of this character would predict measurable national team quality decline in the

604 2030s unless reversed.

605 Figure 3 shows historical registration trajectories and geometric extrapolations to 2042  
606 for the five largest European football nations.

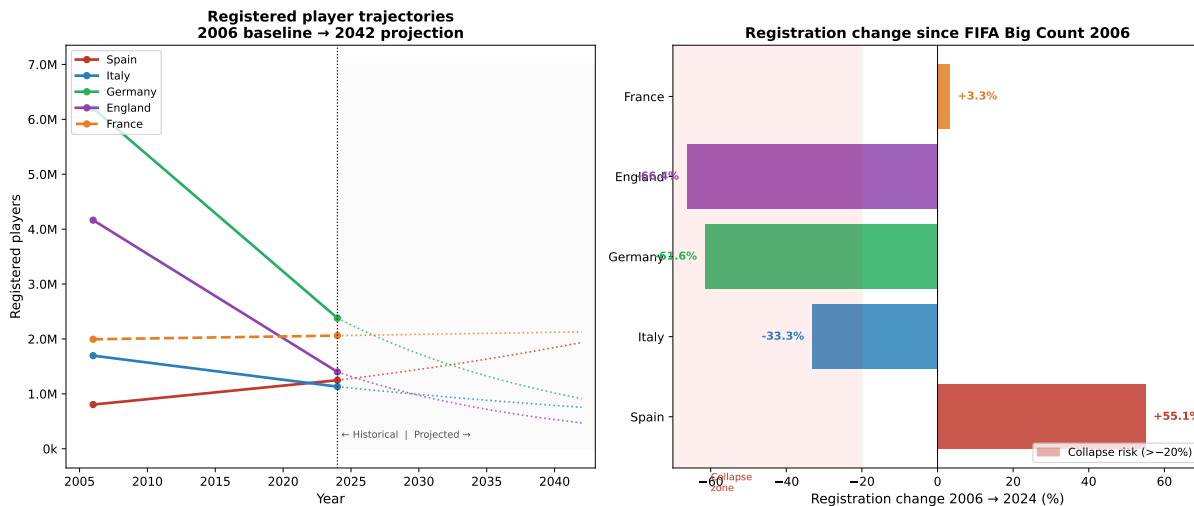


Figure 3: **Registered player trajectories and structural collapse risk.** *Left:* Historical registrations (2006 FIFA Big Count baseline; 2024 federation figures) with geometric projection to 2042 (dotted lines). *Right:* Nominal percentage change 2006–2024 by nation. Italy shows a  $-33.3\%$  change between FIFA Big Count 2006 and FIGC 2025 active figures; Germany has declined from its FIFA Big Count baseline; France is stable. Note: direct comparison of 2006 FIFA Big Count and 2024 federation figures is subject to definitional differences between sources; the figures shown should be treated as indicative of trend direction rather than precise magnitudes.

## 607 5.4 Early Selection, Relative Age Effect, and the Limits of 608 Academy-Only Development

609 Before developing the empirical critique that follows, the scope of the argument deserves  
610 clear statement. Academies develop players who have already cleared significant iden-  
611 tification thresholds, and they do useful work in that role. The claim advanced here is  
612 narrower than a categorical critique of academy systems. It is that an academy-only model  
613 is unlikely to produce a sustainable increase in top talent — because academies select  
614 from an underlying distribution they do not themselves generate — and that under a  
615 binding investment constraint, mean-shifting interventions dominate academy expansion  
616 in expected return, because professional output is a convex function of the population  
617 mean. Where both can be funded, both should be. Where only one can, the analysis

618 below indicates which.

619 The relative age effect data presented in Section 4.4 can be read as more than a  
620 methodological footnote. The magnitude and distribution of RAE across nations constitutes  
621 evidence about how talent identification systems allocate investment—and about whether  
622 that allocation is efficient.

### 623 **RAE as a measure of selection-system bias**

624 A Q1/Q4 ratio of 1.39 pan-European means that January-born players are 39% more  
625 likely than October-born players of identical underlying ability to reach senior professional  
626 status. This is not a marginal distortion. Expressed as a fraction of Q1 selections, the gap  
627  $(Q_1 - Q_4)/Q_1 \approx 28\%$  corresponds to the share of Q1 admissions that came at the expense  
628 of equally able Q4-born peers under an ability-neutral selection regime. These displaced  
629 players are not randomly distributed across the ability range; they are concentrated in the  
630 upper tail—the players born in Q4 who would have been the best professionals had they  
631 not been cut from elite pathways at age 9 or 12.

632 The implication is that the professional conversion rate, as measured in this study,  
633 *understates* the true ability yield achievable from a given population. Every national *FQ*  
634 estimate in Table 2 is a lower bound on what the population could produce under an  
635 ability-neutral selection system.

### 636 **Academy investment amplifies RAE**

637 The cross-national pattern in RAE magnitude (Table 6) is informative. The nations  
638 with the most formalised elite academy infrastructure—Germany (Q1/Q4 = 2.10), Spain  
639 (1.98), Italy (1.87), Portugal (1.85)—show among the strongest RAEs. Nations with less  
640 formal early-selection pathways—Slovenia (1.38, ns), Bulgaria (1.22, ns), Slovakia (1.24,  
641 ns), Hungary (1.25, ns)—show weak or non-significant RAE. This is consistent with the  
642 mechanism: elite academies create structured annual cohort competition with repeated  
643 selection cut points from age 8 onwards. Each cut point is partially biased by physical  
644 maturity rather than ability. The effect compounds across ten years of development: by

645 the time a player graduates from a German or Spanish academy, they have survived eight  
646 to ten selection rounds each subject to relative age bias.

647 The nations at the bottom of the mean  $FQ$  ranking—Germany (96.5), Turkey (96.7),  
648 Netherlands (97.4), France (97.8)—are disproportionately those with the largest and  
649 most institutionalised academy investments. The nations at the top—Serbia (109.0),  
650 Croatia (107.9), Scotland (106.6), Wales (104.2)—are those with less formal early-selection  
651 infrastructure and correspondingly lower RAEs. This pattern does not establish causation,  
652 but it is the opposite of what the academy investment model would predict if early selection  
653 were efficiently identifying the most talented players.

### 654 **France as a natural experiment**

655 France presents an instructive case. The *Fédération Française de Football* (FFF) has  
656 operated mandatory professional academies since the 1970s and the *Institut National du*  
657 *Football* at Clairefontaine since January 1988 — the most institutionalised development  
658 system in Europe. RAE has been identified and discussed in the academic literature for  
659 over two decades (Musch and Grondin, 2001), and French sports-science research has  
660 produced direct empirical work on the phenomenon within the FFF’s own developmental  
661 ecosystem (Carling et al., 2009; Delorme et al., 2010), including studies of birth-date  
662 effects on anthropometric profiles at Clairefontaine (Carling et al., 2009) and large-scale  
663 analyses of relative age and dropout across the French federation’s full licensed playing  
664 population (Delorme et al., 2010). The result is visible in the data: France’s Q1/Q4 ratio  
665 (1.47) is the lowest among major European nations with mandatory academy systems,  
666 substantially below Germany (2.10) and Spain (1.98).

667 France has not solved the RAE problem, but its sustained institutional effort to  
668 counteract it has measurably reduced it. Critically, this correction occurred *within* an elite  
669 academy framework—by applying research findings to change coach behaviour, selection  
670 criteria, and bio-banding practices. This is consistent with the view that RAE is not  
671 an inevitable consequence of formal youth development but a consequence of age-biased  
672 *selection within* formal development; firmer causal inference would require comparable

673 longitudinal evidence from peer nations.

674       However, France’s mean  $FQ$  remains below the European average (97.8), and its FIFA  
675 ranking is sustained largely by pool depth. Active RAE correction improved France’s  
676 talent identification accuracy without raising its population mean ability—because the  
677 intervention was still targeted at the elite selection funnel rather than at the broader  
678 development environment.

### 679 **Mean-shifting as a structural alternative**

680 The academy model and the mean-shifting model embody different theories of where  
681 development investment is best directed. The academy model assumes talent is scarce,  
682 identifiable early, and best developed through intensive specialist investment concentrated  
683 on a small fraction of the player population. The mean-shifting model assumes that talent  
684 is distributed throughout the population, that early identification is unreliable (as the  
685 RAE evidence demonstrates), and that raising the quality of development for the broad  
686 population generates more professional output per unit of investment than concentrating  
687 resources on an elite few. The two are not mutually exclusive in principle; the question  
688 advanced here is which dominates when investment must be prioritised.

689       These are testable propositions. The cross-national data presented here is consistent  
690 with the mean-shifting model on two independent dimensions:

691     1. **Conversion rate.** High-converting nations (Serbia, Croatia, Scotland) are not the  
692 nations with the most developed academy systems. They are nations where the quality  
693 of broad football culture—technical coaching, competitive club environments, high  
694 participation density relative to population—appears to have shifted the population  
695 mean upward without formal early selection.

696     2. **Relative age effect.** Nations with the most intensive early-selection systems show  
697 the highest RAE, indicating they are systematically discarding a substantial fraction  
698 of their most talented players. Mean-shifting interventions, by definition, do not  
699 create selection funnels and therefore do not generate RAE. Talent that would be  
700 cut from a German academy at U11 for a November birthday continues to develop

701 in a mean-shifting environment, remaining available for professional identification at  
702 18 or 20.

703 The efficiency calculation from Section 2.5 can now be read in a new light. A +3  
704  $FQ$  mean shift is analytically equivalent to 1.7–2.0× participation. But if that mean  
705 shift is achieved partly by recovering the ~ 28% of talent currently being discarded  
706 through RAE-biased selection, the cost of achieving it may be substantially lower than  
707 a ground-up participation expansion. Retraining coaches to delay selection, extending  
708 development windows, and investing in broad-based quality improvement are not obviously  
709 more expensive than building and staffing elite academies. They are, however, structurally  
710 different: they raise the floor rather than identify the peaks.

711 This argument does not imply that elite development has no role. Players who  
712 ultimately perform at the highest levels do benefit from specialist training and high-quality  
713 competition. The critique is specifically of *early* selection—the decision to identify and  
714 concentrate investment on a small cohort at age 8 to 12 before relative age bias has  
715 dissipated and before the true ability distribution has had time to manifest. Delaying that  
716 selection point, while continuing to invest in broad development quality, is the practical  
717 policy implication of the combined mean-shifting and RAE evidence presented here.

## 718 5.5 The Developmental Ecosystem: Why Cruyff Needed the 719 Not-Cruyffs

720 *“I trained three to four hours a week at Ajax when I was little but played three  
721 to four hours every day on the street. Where do you think I learned football?”*  
722 — Johan Cruyff<sup>3</sup>

723 This quote has been widely reproduced in coaching and talent development literature as  
724 evidence for the importance of practice volume—a confirmation of the deliberate practice  
725 hypothesis (Helsen et al., 1998) applied to one of football’s greatest players. The ratio is

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<sup>3</sup>This formulation is widely attributed to Cruyff and consistent with his documented accounts of his own development across multiple interviews and writings (Cruyff, 2016). The exact wording varies across sources; the sentiment is unambiguous.

726 striking: roughly ten times more street football than formal coaching, and the rhetorical  
727 question leaves no doubt about which Cruyff considered formative. This reading is not  
728 wrong, but it extracts only half the lesson. It focuses entirely on what Cruyff did, and  
729 misses entirely the conditions that made what Cruyff did possible.

730 Cruyff was describing his experience from inside an ecosystem. From that vantage point,  
731 the street football felt like *his* practice, because subjectively it was. The other children  
732 were simply the other children. What has gone largely unremarked in the literature that  
733 cites him is that those other children were not the backdrop to his development. They  
734 were its mechanism.

735 The three to four hours a day of street football was not practice *for Cruyff alone*. Every  
736 child on that street was accumulating those same hours. Cruyff's development was not  
737 simply a function of his own inputs but of the quality of the developmental ecosystem he  
738 was embedded in—the hundreds of improving players who constituted his daily adversarial  
739 environment.

740 This maps precisely onto the order statistics framework developed in Section 2.4. The  
741 expected ability of the best player drawn from a population follows directly from the  
742 population mean:

$$\mathbb{E}[X_{(1:P)}] \approx \mu + 15 \Phi^{-1}\left(1 - \frac{1}{P}\right) \quad (9)$$

743 Raising  $\mu$  raises  $\mathbb{E}[X_{(1:P)}]$ . A Cruyff is not produced by finding and cultivating the most  
744 promising 10-year-old; a Cruyff is produced by raising the whole distribution, and emerges  
745 from the elevated top. The street football was not a Cruyff-development programme. It  
746 was a population mean-shift, and the elevated tail produced Cruyff.

#### 747 **What the academy-only model misses**

748 The academy-only model does not claim to replace street football for everyone. It claims  
749 to replace it *for Cruyff alone*: to identify the most promising players early and provide  
750 them with a superior structured environment. This is a coherent theory, and where a  
751 broad developmental base still exists for the academy to compound on, it can work. The  
752 empirical evidence presented in this paper suggests two structural problems with treating

753 it as sufficient on its own.

754 First, it cannot reliably identify Cruyff. The relative age data shows that formal  
755 selection systems systematically confuse physical maturity with ability. The player selected  
756 at age nine as the most promising in his cohort is disproportionately likely to have been  
757 born in January. Cruyff, born April 25th—Q2—would survive early selection in most  
758 European systems, but a substantial fraction of equally talented Q4-born peers would  
759 not. Independent evidence supports the limited predictive validity of early elite selection:  
760 [Herrebrøden and Bjørndal \(2022\)](#) find that participation in U17 and U19 international  
761 fixtures is at best weakly predictive of senior elite participation across multiple European  
762 nations, with only the U21 level showing meaningful signal. [Brustio et al. \(2024\)](#) report  
763 similarly low youth-to-senior transition rates and persistent birthdate skew along the  
764 academy pathway.

765 Second, and more fundamentally, the academy-only model removes Cruyff from the  
766 developmental ecosystem that was generating his three to four hours a day of high-quality  
767 adversarial practice. This is the core insight of the ecological-dynamics tradition in sports  
768 skill acquisition ([Davids et al., 2013](#)): skill emerges from the interaction between performer,  
769 task, and environment, and the environment in this case is the population of co-developing  
770 peers, not a coach in isolation. The street did not need a coach to organise it; it was  
771 self-organising in the sense that participation, motivation, and embedding in the peer  
772 group did not need to be supplied externally. When the most promising players are  
773 extracted into academies, the developmental ecosystem does not continue at the same level  
774 for those left behind—it degrades. The not-Cruyffs, who were the essential developmental  
775 environment for Cruyff, are no longer accumulating those hours at the same quality. Under  
776 this account, the next generation's Cruyff would be developing against a thinner, less  
777 competitive informal environment because the academy has extracted the best players  
778 from it.

## 779 **The investment misallocation**

780 The economic logic of elite academy investment is to concentrate resources on the players  
781 most likely to generate return. Under the assumption that talent is identifiable early, this  
782 is rational. But if the primary driver of elite player development is the quality of the  
783 *ecosystem*—not the quality of the resources directed at any individual—then concentration  
784 is precisely the wrong strategy. Investing in the quality of coaching, facilities, and  
785 competitive environment for the broad population raises the mean of the distribution.  
786 This raises not only the number of players above the professional threshold but also the  
787 quality of the developmental environment experienced by every player in it, including the  
788 future Cruyff.

789 The street football cost nothing. Its modern equivalent—accessible club environments,  
790 well-coached recreational leagues, broad technical development programmes—costs sub-  
791 stantially less per participant than elite academies, while reaching the entire distribution  
792 rather than the selected few. The efficiency advantage of mean-shifting over participation  
793 expansion (Section 2.5) should therefore be understood as a lower bound: it assumes the  
794 mean shift is achieved at equivalent cost to participation expansion. If broad-based quality  
795 investment is cheaper per player than elite academy investment—as the evidence from the  
796 highest-converting nations suggests—the efficiency advantage is correspondingly larger.

797 These choices were not abstract for Cruyff himself. After his playing career he reshaped  
798 Barcelona’s youth philosophy, and the approach he embedded at La Masia is widely  
799 credited with producing a generation of technical players including Xavi, Iniesta, Busquets,  
800 and Messi. That academy worked, in part, because it compounded on a broad base of  
801 Catalan and Dutch football that still existed at the time. By the final decades of his life,  
802 however, Cruyff was visibly aware that the broader conditions of his own development were  
803 eroding. The Johan Cruyff Foundation, established in 1997, has since built hundreds of  
804 Cruyff Courts—small public pitches in urban areas—explicitly to recreate the unstructured,  
805 peer-driven environments from which players like him emerged. The arc of his career traces  
806 the argument of this section: a player who emerged from a functioning street ecosystem; a  
807 coach who built an academy that worked because the ecosystem was still there to feed it;

808 and finally a philanthropist who, recognising the ecosystem was disappearing, spent his  
809 final two decades trying to rebuild it.

810 The question a national association should ask is therefore not “how do we develop  
811 Cruyff?” It is “how do we recreate the conditions under which Cruyff developed himself?”  
812 Those conditions were not, in the first instance, a specialist academy. They were a  
813 population in which everyone was playing, everyone was improving, and the best emerged  
814 naturally from the top of an elevated distribution.

## 815 **5.6 Historical Precedent: Population Mean-Shifting in Irish** 816 **Education**

817 The argument that raising a population mean produces disproportionate gains in the right  
818 tail is not merely theoretical. This section draws on Irish educational history as structural  
819 precedent and historical analogy — not as a directly tested causal analysis within this  
820 paper’s dataset, but as an instance of the same mechanism operating at national scale in a  
821 different domain. The parallel is offered to illustrate that the investment logic is not novel  
822 to football, and that its consequences have been observable in real policy history. Ireland  
823 provides a case in which two sequential broad-access interventions produced measurable  
824 changes in high-end output over a generation, while a third intervention with a different  
825 structural character produced a markedly different result.

826 Before 1967, secondary education in Ireland was predominantly fee-paying and socially  
827 selective. A large fraction of the population never progressed beyond primary level. The  
828 free secondary education scheme announced by Donogh O’Malley in September 1966 and  
829 implemented from the 1967/68 school year effectively universalised access to secondary  
830 schooling within a decade: post-primary enrolment rose from approximately 148,000 in  
831 1967 to 239,000 by 1974 ([Fleming et al., 2022](#)). The consequence was not simply that more  
832 Irish people received a moderate education. The distribution of educational attainment  
833 shifted rightward across the whole population. As the base of capable, secondary-educated  
834 citizens deepened, the right tail — the doctors, engineers, academics, lawyers, civil servants,  
835 and entrepreneurs — grew disproportionately. The country became more capable not

836 because it identified the most promising children more accurately, but because it stopped  
837 excluding the vast majority before the distribution had time to develop.

838 The earlier expansion of universal primary education had the same character. Before  
839 universal compulsory primary schooling, a substantial part of the population entered  
840 adult life functionally underdeveloped in ways that capped their contribution regardless of  
841 underlying potential. Removing that constraint raised the floor. The right tail followed.

842 These two expansions are the clearest available examples of the FQ mechanism operating  
843 at national scale in a domain outside sport. In the language of the model: the professional  
844 threshold did not change. What changed was the mean of the distribution below it. And  
845 because professional-level outcomes are tail events, the returns to raising the mean were  
846 disproportionate.

847 The third-level expansion that followed tells a different story, and the contrast is  
848 instructive. Unlike primary and secondary education, tertiary education does not reach the  
849 full population. It is a selective tier. When access to that tier is broadened substantially  
850 without a corresponding rise in the underlying population distribution, the mean quality  
851 within the expanded tier declines. The institution ceases to be the right tail of the distri-  
852 bution and becomes a larger slice of the middle. Furthermore, by weakening the selectivity  
853 of the environment, expansion can reduce the developmental intensity experienced by the  
854 most capable individuals — who now find themselves in an environment less demanding  
855 than it was when entry was more restricted. The right tail is not raised by this process; it  
856 may actually be compressed.

857 The parallel for football is direct. Primary and secondary education are not merely an  
858 analogy for the football development window. For most children in most countries, they *are*  
859 the football development window. The ages at which FQ is formed — approximately five  
860 to eighteen — are the years spent in compulsory education. A national strategy for raising  
861 football FQ therefore cannot be addressed solely through sports federation structures.  
862 It implicates the educational system, the school day, the quality of physical and sport  
863 provision in childhood, and the degree to which football is accessible as a developmental  
864 environment for the whole population during those years. The federation that raises FQ is

865 not the one that builds the best academies. It is the one that ensures the developmental  
866 conditions are in place for the whole under-eighteen population — the football equivalent  
867 of universal primary and secondary education.

## 868 **5.7 Base Expansion versus Elite-Tier Expansion: Opposite Ef-** 869 **fects on the Tail**

870 The Irish education example clarifies a distinction that is easy to miss when thinking  
871 about development investment: base expansion and elite-tier expansion are not merely  
872 different in scale. They are structurally opposite in their effects on the right tail of the  
873 distribution.

874 **Base expansion** operates below the current threshold of meaningful participation.  
875 When a previously excluded population gains access to a developmental environment,  
876 the mean of the whole distribution rises. Because tail probability is a convex function of  
877 the mean (as demonstrated in Section 2.5), the right tail grows disproportionately. More  
878 people become capable; more of the most capable people emerge. This is the mechanism  
879 of universal primary education, of street football ecosystems, of broad improvements in  
880 coaching and club quality across the full playing population.

881 **Elite-tier expansion** operates above a threshold that is already functioning as a  
882 meaningful selector. When the entry standard to an elite programme or institution is  
883 lowered — whether because of deliberate policy, resource pressure, or ambition for scale  
884 — the consequences run in the opposite direction. The mean of the elite group declines.  
885 But more importantly, the developmental environment experienced by the most capable  
886 individuals deteriorates. They are now surrounded by peers of lower average quality than  
887 before. The expectations and norms of the environment soften. The competitive intensity  
888 that the most talented players require to develop against is reduced. The result is not  
889 merely that the elite label becomes less exclusive. The model implies, and the structural  
890 logic suggests, that the right tail of outcomes can be suppressed by degradation of the very  
891 environment that was supposed to produce it. This inference is theoretically grounded  
892 in the peer-quality and developmental intensity mechanisms described above; it is not

893 directly tested in this paper’s cross-sectional dataset, and longitudinal evidence would be  
894 required to establish it causally.

895 This is not a peripheral consideration for football. The academy system in most  
896 European countries has expanded substantially over the past two decades. More clubs  
897 operate academies, more age groups are covered, more players carry “elite” status at  
898 younger ages. If this expansion has occurred without a corresponding improvement in  
899 the underlying population distribution — if it represents elite-tier inflation rather than  
900 base development — then the model suggests the effect on genuine right-tail output may  
901 have been negative rather than positive, even if the relationship has not yet been directly  
902 estimated.

903 The cross-national data are consistent with this concern. The nations that have most  
904 heavily institutionalised early elite selection (Germany, Spain, Italy) sit at the bottom of  
905 the mean  $FQ$  ranking. The nations with the highest professional conversion rates (Serbia,  
906 Croatia, Scotland) are not those with the most developed formal early pathways. This  
907 does not establish causation. But it is the opposite of the pattern one would expect if elite  
908 academy expansion were the primary driver of right-tail football output.

909 The practical implication is precise: investment that expands the developmental  
910 environment below the professional threshold moves the distribution in the right direction.  
911 Investment that expands the category of players labelled elite without a corresponding  
912 strengthening of the base may move it in the wrong direction. A national association  
913 operating under resource constraints faces a genuine choice between these two strategies.  
914 The  $FQ$  framework and the historical evidence presented here consistently point in the  
915 same direction: investment below the threshold moves the distribution; investment above  
916 it, without first strengthening the base, may not. The precise magnitude of this difference  
917 remains an empirical question that comparative cost data and longitudinal designs could  
918 address, but the directional implication of the model is clear.

## 919 5.8 The Abroad Rate as a Leading Indicator

920 The regression evidence (Section 4.2) shows that abroad count is a stronger predictor of  
 921 FIFA ranking than pool size. This is consistent with a *quality amplification* interpretation:  
 922 players who succeed abroad are concentrated in the upper tail of the ability distribution,  
 923 and their frequency signals the location of that tail. Nations with high abroad rates are  
 924 drawing deep into their ability distribution; nations with low abroad rates (Turkey 9%,  
 925 Romania 12%) either have limited competitive access to European labour markets or have  
 926 structural barriers to international mobility.

927 The abroad count may function as a *leading indicator* of national team strength.  
 928 Because players peak at senior professional age and the FIFA ranking reflects current  
 929 national team performance, there should be a lagged relationship: the cohort of 22–28 year  
 930 olds currently playing abroad will constitute the national team of the next 5–10 years.

931 A preliminary test of this hypothesis is possible from historical expatriate-count data  
 932 in CIES Monthly Reports Nos. 75, 85 and 95 (CIES Football Observatory, 2024), which  
 933 between them publish 2017 and 2020 baseline expatriate counts for the top-20 origin  
 934 nations by absolute change. Of these, thirteen are European nations within the present  
 935 sample. Table 8 reports the correlations between abroad counts at three lag lengths and  
 936 the April 2026 FIFA ranking.

Table 8: **Lagged abroad-count correlations with April 2026 FIFA ranking.** Sample restricted to European nations with verifiable historical CIES data. Dependent variable: –FIFA rank. Spearman coefficients are reported in parentheses.

Predictor	Lag	$n$	Pearson $r$ ( $p$ )	Spearman $\rho$ ( $p$ )
log(abroad 2017)	9 years	13	+0.50 (0.08)	+0.52 (0.07)
log(abroad 2020)	6 years	10	+0.53 (0.12)	+0.55 (0.10)
log(abroad 2024)	2 years	13	+0.60 (0.03)	+0.66 (0.02)

937 The pattern is what the leading-indicator hypothesis predicts: the 2017 abroad count,  
 938 separated from the dependent variable by nine years — roughly a full senior-cohort cycle  
 939 — correlates with current FIFA ranking at  $r = +0.50$ . The correlation strengthens as the

940 lag shortens, but the nine-year-lagged predictor retains the majority of the signal of the  
941 two-year-lagged one. A simple OLS confirms the bivariate result: the 2017 expatriate  
942 count alone explains 18% of the variance in current ranking ( $\text{adj-}R^2 = 0.18$ ,  $\hat{\beta} = +11.4$ ,  
943  $p = 0.08$ ), compared with 31% for the concurrent count.

944 Three caveats apply. The sample is small ( $n = 13$ ); the available historical data are  
945 sample-selected on absolute change, biasing the included nations toward those active at  
946 the export margin; and the 2017 counts for Norway, Austria and Serbia were derived from  
947 percentage-change figures rather than read directly. The direction, sign, and magnitude of  
948 the correlation are nonetheless consistent with the leading-indicator interpretation, and a  
949 complete test using the 2017 origins tables for the full 29-nation sample is left to future  
950 work.

## 951 **5.9 The European Labour Market and Threshold Validity**

952 A central concern about any threshold model is whether the threshold is economically  
953 meaningful. We have argued that EU free movement and the Bosman ruling create a  
954 continental arbitrage market. Supporting evidence includes the wide variation in abroad  
955 rates (9–73%) and the fact that nations with high mean  $FQ$  — Croatia (56%), Portugal  
956 (55%), Slovenia (46%), Serbia (45%) — export the majority or near-majority of their  
957 professionals despite small domestic leagues. The pattern is not confined to small high-  
958 mean nations: France, with the deepest domestic pool in the dataset and a below-average  
959 mean  $FQ$ , nonetheless exports 73% of its senior professionals, the highest abroad share  
960 in Europe. Across both ends of the size distribution, the labour market clears on ability  
961 rather than nationality.

962 The calibration approach (using pan-European conversion rate to set  $T$ ) implicitly treats  
963 the European professional ecosystem as a single labour market. This is a simplification:  
964 leagues differ in quality, squad size regulations, and work permit requirements. The UEFA  
965 coefficient system provides a quality-weighted alternative that could be incorporated in  
966 future refinements. However, for the purpose of comparing national development efficiency,  
967 the unweighted threshold provides a sufficient first-order approximation.

## 968 5.10 Towards Individual FQ Measurement

969 The *FQ* framework as developed in this paper is a *population-level latent construct*: national  
970 mean *FQ* is inferred backwards from professional conversion rates rather than measured  
971 directly in individuals. The logic is analogous to estimating a country’s average cognitive  
972 ability from the proportion of its population that becomes research scientists, rather than  
973 from individual test scores. This approach is tractable with available data and produces  
974 testable predictions, but it leaves the normality assumption untested,  $\sigma$  assumed rather  
975 than estimated, and the professional threshold  $T$  calibrated on labour-market outcomes  
976 rather than measured ability.

977 Theoretically, *FQ* could be operationalised as an individual measurement instrument in  
978 the same way that IQ is assessed through a validated multi-domain test battery. Football  
979 ability is multi-dimensional, and a credible *FQ* battery would need to span at minimum  
980 four domains: *technical* (ball control, passing accuracy, and first-touch quality under  
981 varying pressure conditions); *physiological* (speed, agility, endurance, and recovery rate);  
982 *psychological* (in-match competitive temperament, resilience under failure, and coachability,  
983 but also the broader dispositional and lifestyle factors that operate above the professional  
984 threshold: willingness to relocate, tolerance of contract instability and repeated rejection,  
985 discipline around training and recovery in low-supervision environments, and sustained  
986 motivation under uncertainty); and *tactical-cognitive* (decision-making speed, spatial  
987 scanning, pattern recognition, and positional anticipation). The relative weightings of these  
988 domains are not fixed across levels of the game. Physical factors are more discriminating  
989 at younger ages and lower levels; tactical-cognitive factors become progressively more  
990 important as physical differences between players at a given tier narrow; and the broader  
991 psychological and lifestyle weighting is itself tier-dependent — minimal at recreational  
992 and youth levels, increasingly load-bearing as the tier rises, and decisive at and above the  
993 professional cutoff, where the bundle that the labour market actually selects on includes  
994 attributes that have no analogue in youth-academy assessment.

995 Three methodological requirements would need to be satisfied before such a battery  
996 could support the claims made in this paper. First, *domain decomposition*: factor-analytic

997 work to identify which components are necessary and sufficient at each level, and whether a  
998 single general factor — analogous to  $g$  in cognitive ability research — underlies performance  
999 across domains. Second, *level-specific calibration*: validation that battery scores predict  
1000 professional attainment when tested in youth and amateur populations, not merely that  
1001 they correlate with current performance at a given level. Third, *longitudinal validation*:  
1002 prospective cohort studies following tested players to professional outcomes, ideally across  
1003 multiple nations to test whether the scale is cross-culturally stable.

1004 This is a substantial research programme in its own right, extending well beyond the  
1005 scope of the present paper. Its value to the framework, however, would be considerable.  
1006 Direct individual measurement would allow the normality assumption to be tested em-  
1007 pirically rather than assumed;  $\sigma$  to be estimated per country rather than fixed; and the  
1008 threshold  $T$  to be validated against measured individual scores rather than inferred from  
1009 conversion rates. Most consequentially for the talent identification literature, a validated  
1010  $FQ$  battery would allow selection on measured ability rather than on physical maturity and  
1011 birth month, removing the mechanism that produces the relative age effect at source. The  
1012 present paper is best understood as establishing the population-level framework and the  
1013 policy logic that follows from it; individual  $FQ$  measurement is the empirical programme  
1014 that would ultimately place that framework on fully direct evidential foundations.

1015 A practical first step towards threshold calibration does not require the full longitudinal  
1016 research programme described above. Testing two or three squads competing at the  
1017 minimum tier of professional football would produce an empirical multivariate description  
1018 of the professional threshold without requiring cohort follow-up or prior validation of the  
1019 full scale. Players in such squads have, by definition, cleared the professional threshold —  
1020 they are the living calibration set for  $T$ . The within-squad variation across domains is  
1021 not a complication but an asset: a squad of twenty-five professional players will include  
1022 individuals who cleared the threshold through different combinations of attributes — a  
1023 player with exceptional technical ability and modest physical profile alongside one with  
1024 elite physiological measures and average tactical output. That heterogeneity maps the  
1025 shape of the professional zone in multivariate ability space, revealing the trade-offs and

1026 substitutabilities between domains that constitute “sufficient to be professional” as a  
1027 region rather than a single point.

1028 Such a study would produce an empirically grounded minimum-standard profile: not  
1029 “to be professional you need score  $X$ ” in a single number, but “to be professional you  
1030 need to fall within this region of the technical–physiological– psychological–tactical space.”  
1031 Even if incomplete — calibrated only at the professional floor rather than across the full  
1032 distribution — this would represent a substantive advance. It would allow individual  $FQ$   
1033 assessments to be anchored to real professional benchmarks, provide a practical tool for  
1034 development programmes evaluating player trajectories, and generate the first empirical  
1035 test of whether the professional threshold is best described as a hyperplane, a curved  
1036 surface, or a more complex region in ability space. The data collection required is modest:  
1037 systematic testing of two or three lower-professional squads with a provisional battery  
1038 covering the four domains identified above.

## 1039 **5.11 Sensitivity to the $\sigma$ Assumption**

1040 The implied mean  $FQ$  formula rests on two distributional assumptions: normality and  
1041 a fixed  $\sigma = 15$  across all nations. While the normality assumption is discussed in the  
1042 following section, the  $\sigma$  assumption is in some respects the more consequential one. It  
1043 is borrowed from IQ scaling for interpretability, but it is doing structural work that  
1044 deserves direct examination: if Germany’s ability distribution is genuinely wider than  
1045 Serbia’s — which is plausible if a larger, more heterogeneous player base produces greater  
1046 within-country variance — the ranking of implied national means changes.

1047 A useful analytical observation precedes the sensitivity analysis. Each country’s  
1048 conversion rate  $r_c$  maps to a standardised distance from the professional threshold:

$$z_c = \Phi^{-1}(1 - r_c), \quad \text{so that} \quad \mu_c = T - \sigma_c z_c \quad (10)$$

1049 Serbia’s high conversion rate places it at  $z = 2.44$  standard deviations below the threshold;  
1050 Germany’s low rate places it at  $z = 3.27$ . Because countries with low conversion rates

1051 have larger  $z$  values, they are more sensitive to  $\sigma$  perturbations. A one-unit increase in  $\sigma$   
1052 reduces Germany’s implied mean by 3.27 points but Serbia’s by only 2.44 points. This  
1053 asymmetry has a direct consequence for how  $\sigma$  variation affects the rankings.

1054 Table 9 presents implied  $FQ$  values for selected nations under three scenarios.

Table 9: **Sensitivity of implied mean  $FQ$  to  $\sigma$  assumptions.** Scenario 1: common  $\sigma$  varies uniformly (rankings unaffected by construction). Scenario 2: large nations wider ( $\sigma = 18$ ), small nations narrower ( $\sigma = 12$ ) — the heterogeneity hypothesis. Scenario 3: high-converting nations wider ( $\sigma = 18$ ), low-converting nations narrower ( $\sigma = 12$ ) — the most damaging case for the paper’s rankings.

Country	Scenario 1 (common $\sigma$ )				Scenario 2	Scenario 3		
	$\sigma = 12$	$\sigma = 15$	$\sigma = 18$	$\sigma = 21$	$\sigma_c$	FQ	$\sigma_c$	FQ
Serbia	116.3	109.0	101.6	94.3	12	116.3	18	101.6
Croatia	115.4	107.8	100.3	92.7	12	115.4	18	100.3
Scotland	114.4	106.6	98.8	90.9	12	114.4	18	98.8
Portugal	112.4	104.1	95.8	87.5	12	112.4	18	95.8
England	110.1	101.2	92.4	83.5	18	92.4	12	110.1
Spain	108.2	98.9	89.5	80.2	18	89.5	12	108.2
France	107.4	97.8	88.3	78.7	18	88.3	12	107.4
Germany	106.3	96.5	86.7	76.9	18	86.7	12	106.3

1055 Three results emerge from this analysis.

1056 **Common  $\sigma$  variation does not affect rankings.** Because the ranking of implied  
1057 means is determined entirely by the ranking of  $z_c$  values, and  $z_c$  is independent of  $\sigma$  when  
1058  $\sigma$  is common, Scenario 1 changes the scale of the  $FQ$  axis but leaves every country’s rank  
1059 position identical regardless of whether  $\sigma = 12$  or  $\sigma = 21$ .

1060 **The critic’s specific hypothesis strengthens the headline result.** The natural  
1061 form of the heterogeneity concern is that larger, more diverse nations (Germany, France,  
1062 Spain) have wider ability distributions than smaller, more culturally compact nations  
1063 (Serbia, Croatia, Scotland). Under Scenario 2, assigning  $\sigma = 18$  to large nations and  
1064  $\sigma = 12$  to small nations, Germany’s implied mean falls from 96.5 to 86.7 and Serbia’s

1065 rises from 109.0 to 116.3. The Serbia–Germany gap widens from 12.5 to 29.6 points.  
1066 The hypothesis that motivates the critique, if correct, makes the paper’s central finding  
1067 considerably more pronounced rather than less.

1068 **The damaging scenario requires the opposite assumption.** The configuration  
1069 that would flip the Serbia–Germany ranking is Scenario 3: high-converting small nations  
1070 assigned  $\sigma = 18$  and large nations assigned  $\sigma = 12$ . Under these assumptions Germany  
1071 (106.3) surpasses Serbia (101.6). For this reversal to occur, Serbia’s ability distribution  
1072 would need to be wider than Germany’s — more heterogeneous, not less. This is not  
1073 impossible, but it is the opposite of the heterogeneity argument and lacks an obvious  
1074 theoretical motivation. Furthermore, the breakeven calculation shows that for Germany  
1075 and Serbia to have equal implied means under a common threshold, Germany’s  $\sigma$  would  
1076 need to be  $0.746 \times$  Serbia’s  $\sigma$  — that is, Germany’s distribution would need to be *narrower*,  
1077 not wider.

1078 The  $\sigma$  assumption is therefore consequential, but in a directionally asymmetric way.  
1079 Sensitivity to it runs in the opposite direction from the most natural concern. The  
1080 recommended response for future work is empirical estimation of within-country ability  
1081 variance using Transfermarkt market values as a continuous ability proxy, which would  
1082 allow  $\sigma$  to be estimated rather than assumed. Until such data are available, the common  
1083  $\sigma = 15$  baseline is transparent, testable in principle, and — on the basis of the scenarios  
1084 above — conservative with respect to the paper’s main conclusions.

## 1085 **5.12 A Research Programme: Toward Consistent UEFA-Level** 1086 **Data**

1087 The framework presented here generates testable predictions and policy implications that  
1088 the existing data infrastructure is not built to evaluate at the precision the framework  
1089 can in principle deliver. FIFA Big Count is a heterogeneous one-off exercise from 2006;  
1090 federation registration figures use inconsistent definitions of who counts as an active player;  
1091 Transfermarkt is a community-maintained secondary source with unknown systematic  
1092 coverage gaps; CIES reports cover players abroad but not domestic conversion rates. The

1093 framework gives UEFA and its member federations a quantitative reason to coordinate a  
1094 more consistent dataset. We set out the components of that data effort here.

1095 **Standardised registration definitions.** The single most consequential limitation  
1096 in this paper is heterogeneity in what national federations report as “registered” or  
1097 “active” players. A coordinated effort would specify common definitions for activity  
1098 threshold (number of matches per year), age range, competition level, and the distinction  
1099 between licensed players, casual participants, and administrative members. With consistent  
1100 definitions, the denominator in every conversion-rate calculation becomes meaningful in a  
1101 way it currently is not.

1102 **Pan-European player-tracking dataset.** Federation-validated, with known cov-  
1103 erage, including player-level birth date, club, league level, transfer history, and contract  
1104 status. FIFA’s Transfer Matching System (TMS) holds much of this already but is not  
1105 accessible for research use. A research-purpose extract, appropriately anonymised, would  
1106 replace the Transfermarkt-scraped data on which this paper relies and would close the  
1107 largest single source of measurement uncertainty in the implied mean  $FQ$  estimates.

1108 **Longitudinal cohort tracking.** The leading-indicator hypothesis (abroad counts  
1109 predicting future FIFA performance), the structural-collapse prediction (15–20-year lag  
1110 from registration declines), and the conversion-rate dynamics that motivate national  
1111 strategy are all currently untestable because the data is cross-sectional. Annual federation  
1112 reporting in a consistent format would yield a panel within five years that supports causal  
1113 inference where the present paper can only describe correlations.

1114 **Standardised RAE reporting.** Birth-month distributions by federation, age cohort,  
1115 and tier, reported annually. This is the lightest-weight component of the programme and  
1116 would allow the academy-effect analysis in Section 5.4 to be evaluated longitudinally as  
1117 federations adopt or reject RAE-correction practices.

1118 **Individual  $FQ$  threshold calibration.** The programme outlined in Section 5.10:  
1119 a four-domain test battery applied at minimum to two or three lower-tier professional  
1120 squads, producing an empirically grounded multivariate description of the professional  
1121 threshold. This is the smallest data collection in the programme and the one with the

1122 highest framework-tightening return per unit effort.

1123 **Within-country ability variance estimation.** Transfermarkt market values, prop-  
1124 erly cleaned, can serve as a continuous ability proxy for estimating  $\sigma$  per country rather  
1125 than assuming a common value. This is computable from existing data with appropriate  
1126 methodology and would directly address the sensitivity discussion in Section 5.11.

1127 Taken together, these components would convert the framework from a structure  
1128 applied to incomplete cross-sectional data into a measurement system applied to a coherent  
1129 panel. The first three components require institutional coordination through UEFA or a  
1130 comparable body; the last three are within the reach of academic research groups working  
1131 with available data and modest field collection. The framework presented in this paper  
1132 gives UEFA and its member federations a quantitative basis on which to want such a  
1133 dataset, and gives researchers a clear specification of what to build with it.

### 1134 **5.13 Implications for National Associations**

1135 The framework's qualitative results translate into a small number of strategic recommen-  
1136 dations that hold across plausible refinements to the underlying data.

1137 **Prioritise mean-shifting once a reasonable participation base exists.** The  
1138 efficiency calculation in Section 2.5 establishes that a +3 *FQ* shift in the population mean  
1139 is equivalent to a 1.7–2.0× expansion of the participating population, with the multiplier  
1140 rising as the nation moves further below the threshold. For associations that already have  
1141 a broad participation base relative to their population, additional registration growth offers  
1142 diminishing returns; investment in the average quality of development — coaching density,  
1143 coaching quality, RAE-correction practices, holistic rather than early-selection development  
1144 pathways — will produce larger increases in professional output at comparable cost. For  
1145 associations with small or shrinking participation bases, building the base remains a  
1146 prerequisite, but the strategic horizon should treat base expansion as a precondition for  
1147 mean-shifting rather than as the end goal.

1148 **Set conversion-rate targets, not registration targets.** Registration numbers  
1149 measure the denominator; professional output measures success. Federations that monitor

1150 only registration counts can register growth in the base while their conversion rate falls  
1151 — the structural dilution mechanism described in Section 5.7. Conversion-rate targets,  
1152 benchmarked against the pan-European rate of approximately 1.17 per 1,000 active players,  
1153 give a single metric that responds correctly to interventions on either margin.

1154 **Monitor the abroad rate as a leading indicator.** The regression analysis in  
1155 Section 4.2 identified the number of professionals based abroad as the strongest single  
1156 predictor of FIFA ranking ( $\text{adj-}R^2 = 0.502$ ). The abroad rate also responds faster  
1157 than domestic output to changes in cohort quality, because the European labour market  
1158 arbitrages on individual ability rather than nationality. A sustained decline in abroad-based  
1159 professionals from a given cohort is an early warning that the underlying  $FQ$  distribution  
1160 is moving down, observable years before domestic league composition reflects the same  
1161 shift.

1162 **Distinguish small-nation and large-nation strategies.** The size premium derived  
1163 in Section 4.3 implies that a small high-mean nation and a large low-mean nation can  
1164 produce comparable senior national team strength while requiring entirely different devel-  
1165 opment approaches. Small nations cannot brute-force their way to a deep talent pool by  
1166 expanding participation alone; their realistic route to competitive depth runs through high  
1167 mean  $FQ$  and selective elite production. Large nations have pool-size advantages that  
1168 compound only weakly under low conversion rates; their realistic route to performance  
1169 runs through raising the mean of their already-large base, which the size premium then  
1170 amplifies. Imitating the development model of a structurally different nation will tend to  
1171 underperform the model native to one's own size class.

1172 These recommendations are deliberately framed at the level of strategic direction  
1173 rather than operational detail. The framework constrains what the direction should  
1174 be; the operational specifics — which coaching curriculum, which academy structure,  
1175 which selection-bias correction mechanism — are empirical questions that the research  
1176 programme in Section 5.12 would put on a quantitative basis.

1177 A timing caveat applies. To the extent the population mean is itself partly the  
1178 cumulative outcome of past professional output (visible role models, returning professionals

1179 seeding coaching networks, peer-effect compounding; see the endogeneity note in the  
1180 Limitations subsection below), interventions that successfully shift the mean should be  
1181 expected to compound over multi-decade horizons rather than show their full effect within a  
1182 single cohort. National associations evaluating mean-shifting interventions should therefore  
1183 treat the relevant outcome window as fifteen to twenty years rather than one Olympic or  
1184 World Cup cycle.

## 1185 5.14 Limitations

1186 **Normality assumption.** The *FQ* framework assumes a symmetric unimodal ability  
1187 distribution. If the true distribution is skewed or bimodal (e.g., a distinct elite subpopu-  
1188 lation), the threshold calculations will be biased. As noted in Section 2, the qualitative  
1189 efficiency conclusions require only monotone tails, not normality per se. Empirical testing  
1190 of the distributional assumption using Transfermarkt market values as a proxy for ability  
1191 is a natural extension.

1192 **Registration data heterogeneity.** The most consequential methodological limitation  
1193 is heterogeneity in what national federations report as “registered players.” England’s 1.4  
1194 million figure includes all grassroots participants; Portugal’s 235,000 reflects only federated  
1195 competitive players. This inconsistency means cross-country comparisons of conversion  
1196 rates are confounded with registration methodology. We have addressed this partially  
1197 through the conflation correction and confidence levels, but the underlying data quality  
1198 varies by nation. Serbia and Slovakia receive LOW confidence ratings, and their *FQ*  
1199 estimates carry the widest confidence intervals.

1200 **Cross-sectional design.** National *FQ* estimates are cross-sectional for the 2024/25  
1201 season and reflect the current stock of professionals, not the flow that generated them.  
1202 The lagged-correlation analysis in Section 5.8 provides preliminary historical evidence  
1203 using CIES Monthly Reports, but is restricted to the thirteen European nations for which  
1204 CIES publishes historical baseline counts. A full historical panel covering all 29 nations  
1205 from 2016 onwards would enable proper longitudinal testing of both the leading-indicator  
1206 hypothesis and the structural collapse prediction.

1207 **Relative age effect bias.** As noted in Section 4.4, the RAE introduces systematic  
1208 bias in the professional conversion rate as an ability proxy. The magnitude of this bias  
1209 differs by nation (Q1/Q4 ratios range from 1.21 to 2.13 across countries with significant  
1210 RAEs). Countries with high RAE will have slightly inflated mean  $FQ$  estimates relative  
1211 to true underlying ability, because their professional player cohort is partially selected on  
1212 birthdate rather than ability.

1213 **Gender exclusion.** The analysis covers male players only, reflecting both data  
1214 availability constraints and the current structure of the European professional labour  
1215 market. The mean-shifting framework applies in principle to female football as well, but  
1216 the threshold, conversion rates, and registration denominators would require separate  
1217 estimation.

1218 **What is robust and what is not.** The preceding limitations bear unevenly on  
1219 different parts of the contribution. Exact national point estimates of mean  $FQ$  are the  
1220 most sensitive component: a federation that under- or over-counts its active base by  
1221 30–50% will see its implied mean shift by several  $FQ$  points, which is enough to change  
1222 neighbouring positions in the ranking. The qualitative results of the framework are not  
1223 similarly fragile. The mean-shifting efficiency calculation (Section 2.5) depends only on  
1224 the threshold geometry of a tail distribution, not on any particular country’s denominator.  
1225 The size premium is a direct consequence of order statistics on bounded samples and  
1226 is independent of registration accuracy. The pattern that small high-conversion nations  
1227 (Serbia, Croatia, Iceland, Scotland) cluster above large low-conversion nations (Germany,  
1228 France, Netherlands) is visible in raw conversion rates before any modelling, and Section 5.2  
1229 shows that overturning this pattern would require implausibly large adjustments to the  
1230 denominators of multiple countries simultaneously. The framework, the efficiency result,  
1231 and the broad ranking direction should therefore be read as the durable contribution;  
1232 exact point estimates should be read as illustrative pending the coordinated UEFA-level  
1233 data effort described in Section 5.12.

1234 **Endogeneity of the mean.** A final caveat concerns the direction of causation. The  
1235 framework treats the population mean  $FQ$  as a parameter that interventions target, but a

1236 strong professional pipeline is itself plausibly a cause of mean  $FQ$  growth in subsequent  
1237 generations: visible role models raise participation intensity, returning professionals seed  
1238 coaching networks, and competitive academy infrastructure raises the quality of practice  
1239 available to the next cohort. The broader economics of education literature documents  
1240 non-trivial peer-effect and role-model channels in skill acquisition contexts (Sacerdote,  
1241 2011), and there is no a priori reason to expect the football developmental environment  
1242 to be exempt from such effects. To the extent this feedback operates, cross-sectional  
1243 means partly reflect the cumulative effect of past professional output rather than an  
1244 independent cause of it. This does not invalidate the efficiency result — which is a  
1245 statement about marginal returns to interventions on the mean — but it does imply that  
1246 the gap between high-mean and low-mean nations may be self-reinforcing absent deliberate  
1247 counter-investment, and that successful mean-shifting interventions should compound over  
1248 multi-decade horizons rather than within a single cohort.

## 1249 6 Conclusion

1250 We have introduced the Football Quotient, a framework for quantifying the implied ability  
1251 distribution of national playing populations from professional conversion rates. Applied to  
1252 29 European nations using 2024/25 data, the framework identifies substantial variation in  
1253 national mean  $FQ$ —from Serbia (109.0) to Germany (96.5)—that is largely invisible in  
1254 FIFA rankings but is highly informative about developmental efficiency.

1255 The central analytical result is that raising the population mean  $FQ$  generates dis-  
1256 proportionate increases in professional output because professional status is a threshold  
1257 phenomenon. A +3  $FQ$  point improvement—a small fraction of one standard deviation on  
1258 the  $FQ$  scale—achieves 85–100% of what doubling the participating population achieves,  
1259 across all national baselines in our dataset. As participation size is generally constrained  
1260 by population and infrastructure, while mean ability is responsive to coaching quality,  
1261 methodology, and development environment, this efficiency comparison is a direct argument  
1262 for quality-first development strategies.

1263 The European Union’s free movement of labour provides an empirical market mechanism

1264 that continuously calibrates the professional threshold, lending ecological validity to the  
1265 model: the threshold is not a statistical artefact but the real minimum level of ability  
1266 required to secure professional employment somewhere in the European football ecosystem.

1267 The decomposition of national team quality into mean  $FQ$  and size premium reveals  
1268 complementary vulnerability profiles. Large nations are insulated by pool depth but face  
1269 structural risk from declining registration trends, with effects emerging on a 15–20 year  
1270 lag. Small nations with high mean  $FQ$  can achieve national team quality comparable to  
1271 large nations through the size premium on a smaller but higher-quality population base.

1272 The empirical estimates in this paper rest on existing data sources whose heterogeneity  
1273 is documented and whose precision is correspondingly bounded. We view this work as  
1274 a precursor to a coordinated UEFA-level data effort that the framework itself motivates:  
1275 standardised registration definitions across federations, federation-validated pan-European  
1276 player tracking, longitudinal cohort series, and individual threshold calibration. Section 5.12  
1277 sets out the components of that effort. The framework presented here gives UEFA and its  
1278 member federations a quantitative basis on which to coordinate such a dataset, and gives  
1279 researchers a clear specification of what to build once it exists.

1280 A preliminary test reported in Section 5.8 shows that the abroad count from 2017 retains  
1281 a Spearman correlation of +0.52 with the April 2026 FIFA ranking across thirteen European  
1282 nations with verifiable historical CIES data, consistent with the leading-indicator prediction;  
1283 a complete test using the full 29-nation sample remains outstanding. This finding is also  
1284 consistent in spirit with [Bernard and Busse \(2004\)](#), whose Olympic production-function  
1285 model shares both the normal-ability assumption and the conclusion that population-scale  
1286 and per-capita quality factors contribute jointly to elite output. The football case provides  
1287 the labour-market mechanism by which the per-capita factor is arbitrated across borders,  
1288 which the Olympic case does not.

1289 Within the existing data, future work should (i) extend the leading-indicator test to  
1290 the full 29-nation sample once historical CIES origin tables become publicly available, (ii)  
1291 test the normality assumption empirically using market value distributions, (iii) extend  
1292 the framework to female football, and (iv) integrate UEFA league quality coefficients to

1293 refine the threshold calibration.

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1360 **A Mathematical Derivation of Mean-Shifting Effi-**  
 1361 **ciency**

1362 Let  $X \sim \mathcal{N}(\mu, \sigma^2)$  denote the ability of a randomly selected active player, and let  $T$  be the  
 1363 professional threshold. The probability of professional attainment is  $p(\mu) = 1 - \Phi\left(\frac{T-\mu}{\sigma}\right)$ ,  
 1364 where  $\Phi$  is the standard normal CDF.

1365 Define the *output multiplier* from a mean shift of  $\Delta$ :

$$\rho(\Delta) = \frac{p(\mu + \Delta)}{p(\mu)} = \frac{1 - \Phi\left(\frac{T-\mu-\Delta}{\sigma}\right)}{1 - \Phi\left(\frac{T-\mu}{\sigma}\right)} \quad (11)$$

1366 Let  $z_0 = (T - \mu)/\sigma$  and  $z_1 = (T - \mu - \Delta)/\sigma = z_0 - \Delta/\sigma$ . Then:

$$\rho(\Delta) = \frac{1 - \Phi(z_1)}{1 - \Phi(z_0)} = \frac{\bar{\Phi}(z_0 - \Delta/\sigma)}{\bar{\Phi}(z_0)} \quad (12)$$

1367 where  $\bar{\Phi} = 1 - \Phi$ .

1368 The log-survival function  $\log \bar{\Phi}(z)$  is strictly convex in  $z$  (the normal hazard rate  
 1369  $\phi(z)/\bar{\Phi}(z)$  is strictly increasing in  $z$ ). Therefore:

$$\log \bar{\Phi}(z_0 - \Delta/\sigma) > \log \bar{\Phi}(z_0) - (\Delta/\sigma) \cdot \left. \frac{d}{dz} \log \bar{\Phi}(z) \right|_{z_0} \quad (13)$$

1370 This means  $\rho(\Delta) > 1$  for all  $\Delta > 0$ , and moreover  $\rho(\Delta)$  grows faster than linearly  
 1371 for large  $\Delta$  (super-linear multiplicative gain). The equivalent participation multiplier is  
 1372 precisely  $\rho(\Delta)$ , and the super-linearity gives the efficiency advantage of mean-shifting over  
 1373 participation expansion. The quantitative values in Table (main text) are obtained by  
 1374 numerical evaluation at  $T = 145.6$ ,  $\sigma = 15$ , and  $\mu \in \{96.5, 100.0, 109.0\}$ .

1375 **B Order Statistics Approximation for National Team**  
 1376 **Quality**

1377 The expected value of the  $k$ -th order statistic (in decreasing order) from a  $\mathcal{N}(\mu, \sigma^2)$  sample  
 1378 of size  $P$  is approximated by:

$$\mathbb{E}[X_{(k:P)}] \approx \mu + \sigma \Phi^{-1}\left(1 - \frac{k}{P+1}\right) \quad (14)$$

1379 using the [Blom \(1958\)](#) plotting position approximation. The national team average  $FQ$   
 1380 (equation 7) sums this over  $k = 1, \dots, 30$ :

$$\overline{FQ}^{\text{NT}} = \mu + \frac{\sigma}{30} \sum_{k=1}^{30} \Phi^{-1}\left(1 - \frac{k}{P+1}\right) \quad (15)$$

1381 For the active population sizes in our dataset (range: 60,334 to 2,380,000), the  $P/(P+1)$   
 1382 correction is negligible and we use  $P$  throughout.

1383 **C Data Sources and Registration Figures**

Table 10: **Registration data sources and confidence ratings.** FIFA BC = FIFA Big Count 2006. Active = estimated active competing population after adjustments. Conf. = confidence level.

Country	FIFA BC	Active	Primary source	Conf.
England	4,164,110	1,400,000	FA activity- adjusted	HIGH
Germany	6,200,000	2,380,000	DFB registered 2024	HIGH
France	1,994,654	2,060,960	FFF registered 2024	HIGH
Italy	1,696,000	1,131,906	FIGC 2025	HIGH

*continued on next page*

*(continued)*

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Country	FIFA BC	Active	Primary source	Conf.
Spain	805,035	1,248,511	RFEF 2024	HIGH
Netherlands	1,212,697	1,100,000	KNVB active 2024	HIGH
Belgium	413,284	400,000	URBSFA 2023	HIGH
Portugal	178,111	235,000	FPF 2024	HIGH
Scotland	161,412	161,412	SFA 2023	HIGH
Norway	391,139	413,139	NFF 2024	HIGH
Denmark	268,402	381,840	DBU 2024	HIGH
Sweden	484,662	379,681	SvFF 2024	HIGH
Switzerland	262,000	273,644	ASF 2023	MED
Austria	270,000	248,000	ÖFB adjusted	MED
Czech Rep.	239,500	358,000	FAČR 2023	MED
Romania	136,000	300,000	MDPI 2023	MED
Greece	93,600	200,000	EPO estimate	MED
Ireland	88,000	220,000	FAI 2023	HIGH
Wales	86,340	105,603	FAW 2023	HIGH
Finland	114,393	150,894	SPL 2024	HIGH
Hungary	186,000	300,000	MLSZ 2023	HIGH
Bulgaria	63,026	120,000	BFU estimate	LOW
Slovenia	29,400	60,334	NZS 2024	MED
Croatia	130,000	118,316	HNS 2023	LOW
Slovakia	51,000	90,000	SFZ estimate	LOW
Serbia	146,845	120,194	FSS 2023	LOW
Ukraine	1,016,000	1,016,000	UAF 2022	LOW
Poland	395,550	769,000	PZPN 2023	LOW
Turkey	985,000	985,000	TFF 2022	LOW

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